

# Package ‘tfCox’

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**Type** Package

**Title** Fits Piecewise Polynomial with Data-Adaptive Knots in Cox Model

**Version** 0.1.0

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**Description** In Cox's proportional hazard model, covariates are modeled as linear function and may not be flexible. This package implements additive trend filtering Cox proportional hazards model as proposed in Jiacheng Wu & Daniela Witten (2019) ``Flexible and Interpretable Models for Survival Data", Journal of Computational and Graphical Statistics, <[DOI:10.1080/10618600.2019.1592758](https://doi.org/10.1080/10618600.2019.1592758)>. The fitted functions are piecewise polynomial with adaptively chosen knots.

**License** GPL (>= 2)

**Imports** Rcpp (>= 0.12.14), survival, stats

**LinkingTo** Rcpp

**NeedsCompilation** yes

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|               |                                                   |
|---------------|---------------------------------------------------|
| tfCox-package | <i>Fit the Additive Trend Filtering Cox Model</i> |
|---------------|---------------------------------------------------|

---

**Description**

This package is called tfCox or trend filtering for Cox model, which is proposed in Jiacheng Wu & Daniela Witten (2019) Flexible and Interpretable Models for Survival Data, Journal of Computational and Graphical Statistics, DOI: 10.1080/10618600.2019.1592758. It provides an approach to fit additive Cox model in which each component function is estimated to be piecewise polynomial with adaptively-chosen knots.

Function [tfCox](#) fits the trend filtering Cox model for a range of tuning parameters. Function [cv\\_tfCox](#) returns the optimal tuning parameter selected by K-fold cross validation.

**Details**

Package: tfCox  
Type: Package  
Version: 0.1.0  
Date: 2019-05-20  
License: GPL (>= 2)

The package includes the following functions: [tfCox](#), [cv\\_tfCox](#), [plot.tfCox](#), [plot.cv\\_tfCox](#), [predict.tfCox](#), [summary.tfCox](#), [summary.cv\\_tfCox](#), [sim\\_dat](#), [plot.sim\\_dat](#).

**Author(s)**

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**References**

Jiacheng Wu & Daniela Witten (2019) Flexible and Interpretable Models for Survival Data, Journal of Computational and Graphical Statistics, DOI: 10.1080/10618600.2019.1592758

cv\_tfCox

---

*Fit Trend Filtering Cox model and Choose Tuning Parameter via K-Fold Cross-Validation*


---

## Description

Fit additive trend filtering Cox model where each component function is estimated to be piecewise constant or polynomial. Tuning parameter is selected via k-fold cross-validation.

## Usage

```
cv_tfCox(dat, ord=0, alpha=1, discrete=NULL, lambda.seq=NULL,
lambda.min.ratio=0.01, n.lambda=30, n.fold=5, seed=NULL, tol=1e-6,
niter=1000, stepSize=25, backtracking=0)
```

## Arguments

|                  |                                                                                                                                                                                                                                                                                                                                                                                                                             |
|------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| dat              | A list that contains time, status and X. time is failure or censoring time, status is censoring indicator, and X is n x p matrix and may have $p > n$ .                                                                                                                                                                                                                                                                     |
| ord              | The polynomial order of the trend filtering fit; a non-negative interger (ord $\geq$ 3 is not recommended). For instance, ord=0 will produce piewise constant fit, ord=1 will produce piewise linear fit, and ord=2 will produce piewise quadratic fit.                                                                                                                                                                     |
| alpha            | The trade-off between trend filtering penalty and group lasso penalty. It must be in [0,1]. alpha=1 corresponds to the case with only trend filtering penalty to produce piecewise polynomial, and alpha=0 corresponds to the case with only group lasso penalty to produce sparsity of the functions. alpha between 0 and 1 is the tradeoff between the strength of these two penalties. For $p < n$ , we suggest using 1. |
| discrete         | A vector of covariate/feature indice that are discrete. Discrete covariates are not penalized in the model. Default NULL means that none of the covariates are discrete thus all covariates will be penalized in the model.                                                                                                                                                                                                 |
| lambda.seq       | The sequence of positive lambda values to consider. The default is NULL, which calculates lambda.seq using lambda.min.ratio and n.lambda. If lambda.seq is provided, it will override the default. lambda.seq should be a decreasing positive sequence of values since cv_tfCox relies on warm starts to speed up the computation.                                                                                          |
| lambda.min.ratio | Smallest value for lambda.seq, as a fraction of the maximum lambda value, which is the smallest value such that the penalty term is zero. The default is 0.01.                                                                                                                                                                                                                                                              |
| n.lambda         | The number of lambda values to consider. Default is 30.                                                                                                                                                                                                                                                                                                                                                                     |
| n.fold           | The number of folds for cross-validation of lambda. The default is 5.                                                                                                                                                                                                                                                                                                                                                       |
| seed             | An optional number used with set.seed().                                                                                                                                                                                                                                                                                                                                                                                    |

|              |                                                                                  |
|--------------|----------------------------------------------------------------------------------|
| tol          | Convergence criterion for estimates.                                             |
| niter        | Maximum number of iterations.                                                    |
| stepSize     | Initial step size. Default is 25.                                                |
| backtracking | Whether backtracking should be used 1 (TRUE) or 0 (FALSE). Default is 0 (FALSE). |

### Details

Note that `cv_tfCox` does not cross-validate over  $\alpha$ , and  $\alpha$  should be provided. However, if the user would like to cross-validate over  $\alpha$ , then `cv_tfCox` should be called multiple times for different values of  $\alpha$  and the same seed. This ensures that the cross-validation folds (fold) remain the same for the different values of  $\alpha$ . See the example below for details.

### Value

An object with S3 class "cv\_tfCox".

|                            |                                                                                          |
|----------------------------|------------------------------------------------------------------------------------------|
| <code>best.lambda</code>   | Optional lambda value chosen by cross-validation.                                        |
| <code>lambda.seq</code>    | lambda sequence considered.                                                              |
| <code>mean.cv.error</code> | vector of average cross validation error with the same length as <code>lambda.seq</code> |

### Author(s)

Jiacheng Wu

### References

Jiacheng Wu & Daniela Witten (2019) Flexible and Interpretable Models for Survival Data, Journal of Computational and Graphical Statistics, DOI: 10.1080/10618600.2019.1592758

### See Also

[summary.cv\\_tfCox](#), [plot.cv\\_tfCox](#), [tfCox](#)

### Examples

```
#generate data
set.seed(123)
dat = sim_dat(n=100, zero=0, scenario=1)

#fit piecewise constant functions
#cross-validation to choose the tuning parameter lambda with fixed alpha=1
cv = cv_tfCox(dat, ord=0, alpha=1, n.fold=2, seed=123)
plot(cv, showSE=TRUE)
```

---

`negloglik`*Calculate the negative log likelihood from Cox model.*

---

**Description**

Calculate the negative log likelihood from Cox model from the estimated coefficient matrix theta.

**Usage**

```
negloglik(dat, theta)
```

**Arguments**

|                    |                                                                                                                                                         |
|--------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------|
| <code>dat</code>   | A list that contains time, status and X. time is failure or censoring time, status is censoring indicator, and X is n x p matrix and may have $p > n$ . |
| <code>theta</code> | An n x p matrix of coefficients corresponding to covariates X.                                                                                          |

**Author(s)**

Jiacheng Wu

**References**

Jiacheng Wu & Daniela Witten (2019) Flexible and Interpretable Models for Survival Data, Journal of Computational and Graphical Statistics, DOI: 10.1080/10618600.2019.1592758

**See Also**

[predict\\_best\\_lambda](#), [tfCox\\_choose\\_lambda](#)

**Examples**

```
#generate training and testing data
dat = sim_dat(n=100, zero=0, scenario=1)
test_dat = sim_dat(n=100, zero=0, scenario=1)

#choose the optimal tuning parameter
cv = tfCox_choose_lambda(dat, test_dat, ord=0, alpha=1)
plot(cv$lam_seq, cv$loss)

#optimal tuning parameter
cv$best_lambda

#predict the coefficients of testing covariates from the optimal tuning parameter
#from tfCox_choose_lambda object.
theta_hat = predict_best_lambda(cv, test_dat$X)

#calculate the loss in the testing data based on the estimated coefficients theta
negloglik(test_dat, theta_hat)
```

---

`plot.cv_tfCox`*Plots Cross-Validation Curve for Object of Class "cv\_tfCox"*

---

### Description

This function plots the cross-validation curve for models fitted by a range of tuning parameter lambda using `cv_tfCox`. The cross-validation error with  $\pm 1$  standard error is plotted for each value of lambda. The dotted vertical line indicates the chosen lambda corresponding to the minimum cross-validation error.

### Usage

```
## S3 method for class 'cv_tfCox'
plot(x, showSE=F, ...)
```

### Arguments

|                     |                                                                                          |
|---------------------|------------------------------------------------------------------------------------------|
| <code>x</code>      | an object of class "cv_tfCox"                                                            |
| <code>showSE</code> | a logical (TRUE or FALSE) for whether the standard errors of the curve should be plotted |
| <code>...</code>    | additional arguments to be passed. These are ignored in this function.                   |

### Author(s)

Jiacheng Wu

### See Also

[cv\\_tfCox](#)

### Examples

```
#generate data
set.seed(123)
dat = sim_dat(n=100, zeroF=0, scenario=1)

#fit piecewise constant functions
#cross-validation to choose the tuning parameter lambda with fixed alpha=1
cv = cv_tfCox(dat, ord=0, alpha=1, n.fold=2, seed=123)
plot(cv, showSE=TRUE)
```

---

|              |                                        |
|--------------|----------------------------------------|
| plot.sim_dat | <i>Plot the true covariate effects</i> |
|--------------|----------------------------------------|

---

## Description

This function plots the functional form of covariate effects in four simulation scenarios.

## Usage

```
## S3 method for class 'sim_dat'  
plot(x, which.predictor = NULL, n.plot = 4, ...)
```

## Arguments

|                 |                                                                                                                                                                     |
|-----------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| x               | an object of class "sim_dat"                                                                                                                                        |
| which.predictor | a vector of predictor index that indicates which predictor function to plot. The vector should have integer values from 1 to p where p is the number of predictors. |
| n.plot          | the number of predictors to be plotted (default is 4). If which.predictor is supplied, this argument is ignored.                                                    |
| ...             | additional arguments to be passed. These are ignored in this function.                                                                                              |

## Author(s)

Jiacheng Wu

## See Also

[sim\\_dat](#)

## Examples

```
#generate data  
set.seed(123)  
dat = sim_dat(n=100, zerof=0, scenario=1)  
#plot X versus the true theta  
plot.sim_dat(dat)
```

plot.tfCox

*Plot Fitted Functions from Class "tfCox"***Description**

This function plots the fitted functions from a model estimated by [tfCox](#).

**Usage**

```
## S3 method for class 'tfCox'
plot(x, which.lambda=1, which.predictor = NULL, n.plot = 4, ...)
```

**Arguments**

|                 |                                                                                                                                                                                                                                                      |
|-----------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| x               | an object of class "tfCox"                                                                                                                                                                                                                           |
| which.lambda    | the index for the model of interest to be plotted. which.lambda corresponds to the model fit in lambda.seq and should be integer between 1 to length(fit\$lambda.seq). In other words, the fit from fit\$theta.list[[which.lambda]] will be plotted. |
| which.predictor | a vector of predictor index that indicates which predictor function to plot. The vector should have integer values from 1 to p where p is the number of predictors.                                                                                  |
| n.plot          | the number of predictors to be plotted (default is 4). Note that only those non-zero estimated functions will be plotted. If which.predictor is supplied, this argument is ignored.                                                                  |
| ...             | additional arguments to be passed. These are ignored in this function.                                                                                                                                                                               |

**Author(s)**

Jiacheng Wu

**See Also**

[tfCox](#)

**Examples**

```
#generate data
set.seed(123)
dat = sim_dat(n=100, zero=0, scenario=1)

fit = tfCox(dat, ord=0, alpha=1, lambda.seq=0.04)
plot(fit, n.plot=4)
```

---

|               |                                                                              |
|---------------|------------------------------------------------------------------------------|
| predict.tfCox | <i>Predict for a New Covariate Matrix and fit from <a href="#">tfCox</a></i> |
|---------------|------------------------------------------------------------------------------|

---

## Description

This function makes predictions from a specified covariate matrix for a fit of the class "tfCox".

## Usage

```
## S3 method for class 'tfCox'  
predict(object, newX, which.lambda=1, ...)
```

## Arguments

|              |                                                                                                                                                                                                                                                      |
|--------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| object       | an object of the class "tfCox"                                                                                                                                                                                                                       |
| newX         | a n x p covariate matrix                                                                                                                                                                                                                             |
| which.lambda | the index for the model of interest to be plotted. which.lambda corresponds to the model fit in lambda.seq and should be integer between 1 to length(fit\$lambda.seq). In other words, the fit from fit\$theta.list[[which.lambda]] will be plotted. |
| ...          | additional arguments to be passed. These are ignored in this function.                                                                                                                                                                               |

## Details

Prediction for the new data point is implemented by constant or linear interpolation. 0th order trend filtering will have constant interpolation, and 1th or higher order trend filtering will have linear interpolation.

## Value

A n x p matrix containing the fitted theta values.

## Author(s)

Jiacheng Wu

## See Also

[tfCox](#)

---

|                     |                                                                 |
|---------------------|-----------------------------------------------------------------|
| predict_best_lambda | <i>Predict from the optimal lambda from tfCox_choose_lambda</i> |
|---------------------|-----------------------------------------------------------------|

---

**Description**

Estimate the corresponding theta values from the optimal tuning parameter obtained by [tfCox\\_choose\\_lambda](#).

**Usage**

```
predict_best_lambda(cv, newX)
```

**Arguments**

|      |                                                      |
|------|------------------------------------------------------|
| cv   | An object from <a href="#">tfCox_choose_lambda</a> . |
| newX | The new covariate values.                            |

**Value**

Estimated theta values.

**Author(s)**

Jiacheng Wu

**References**

Jiacheng Wu & Daniela Witten (2019) Flexible and Interpretable Models for Survival Data, Journal of Computational and Graphical Statistics, DOI: 10.1080/10618600.2019.1592758

**See Also**

[tfCox\\_choose\\_lambda](#), [negloglik](#)

**Examples**

```
#generate training and testing data
dat = sim_dat(n=100, zerof=0, scenario=1)
test_dat = sim_dat(n=100, zerof=0, scenario=1)

#choose the optimal tuning parameter
cv = tfCox_choose_lambda(dat, test_dat, ord=0, alpha=1)
plot(cv$lam_seq, cv$loss)

#optimal tuning parameter
cv$best_lambda

#Estimate the theta values of testing covariates from the optimal tuning parameter
#from tfCox_choose_lambda object.
theta_hat = predict_best_lambda(cv, test_dat$X)
```

sim\_dat

*Simulate Data from a Variety of Functional Scenarios***Description**

This function generates survival data according to the simulation scenarios considered in Section 4 of Wu, J., and Witten, D. (2019) Flexible and interpretable models for survival data. Cox model has the form

$$\lambda(t|x) = \lambda_0(t) \exp\left(\sum_{j=1}^p f_j(x)\right)$$

. Failure time is generated by Weibull distribution with baseline hazard

$$\lambda_0(t) = \text{scale} * \text{shape} * t^{\text{shape}-1}$$

. In the paper, however, failure time is generated by a simplified weibull distribution: exponential(1) baseline hazard corresponding to shape=1 and scale=1. Censoring time is generated independently by exponential distribution with intensity censoring.rate. Thus the observed time is the minimum of failure time and censoring time. Each scenario has four covariates that have some non-linear association with the outcome. There is the option to also generate a user-specified number of covariates that have no association with the outcome.

**Usage**

```
sim_dat(n, zerof=0, scenario=1, scale=1, shape=1, censoring.rate=0.01, n.discrete=0)
```

**Arguments**

|                |                                                                                                                                                                                                                                                                                                                                                                                   |
|----------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| n              | number of observations.                                                                                                                                                                                                                                                                                                                                                           |
| scenario       | Simulation scenario. Options are 1, 2, 3, 4. Scenario 1 corresponds to piecewise constant functions, scenario 2 corresponds to smooth functions, scenario 3 corresponds to piecewise linear functions, and scenario 4 corresponds to functions that have varying degrees of smoothness. Each scenario has four covariates that have some non-linear association with the outcome. |
| zerof          | Number of additional covariates that have no association with the outcome. The total number of covariates is 4+zerof.                                                                                                                                                                                                                                                             |
| scale          | scale parameter as in rweibull                                                                                                                                                                                                                                                                                                                                                    |
| shape          | shape parameter as in rweibull                                                                                                                                                                                                                                                                                                                                                    |
| censoring.rate | censoring intensity. Censoring time is generated by exponential distribution with intensity censoring.rate.                                                                                                                                                                                                                                                                       |
| n.discrete     | The number of binary covariates and default is zero binary covariate.                                                                                                                                                                                                                                                                                                             |

**Value**

|            |                                                                 |
|------------|-----------------------------------------------------------------|
| time       | failure or censoring time whichever comes first.                |
| status     | censoring indicator. 1 denotes censoring and 0 denotes failure. |
| X          | n x p covariate matrix.                                         |
| true_theta | n x p matrix.                                                   |

**Author(s)**

Jiacheng Wu

**References**

Jiacheng Wu & Daniela Witten (2019) Flexible and Interpretable Models for Survival Data, Journal of Computational and Graphical Statistics, DOI: 10.1080/10618600.2019.1592758

**See Also**

[plot.sim\\_dat](#)

**Examples**

```
#generate data
set.seed(123)
dat = sim_dat(n=100, zerof=0, scenario=1)
#plot X versus the true theta
plot.sim_dat(dat)
```

---

summary.cv\_tfCox

---

*Summarize cv\_tfCox object*


---

**Description**

This function summarizes cv\_tfCox object and identifies the tuning parameter chosen by cross-validation.

**Usage**

```
## S3 method for class 'cv_tfCox'
summary(object, ...)
```

**Arguments**

|        |                                                                        |
|--------|------------------------------------------------------------------------|
| object | an object of class "cv_tfCox"                                          |
| ...    | additional arguments to be passed. These are ignored in this function. |

**Author(s)**

Jiacheng Wu

**See Also**

[cv\\_tfCox](#), [plot.cv\\_tfCox](#)

**Examples**

```
#generate data
set.seed(1234)
dat = sim_dat(n=100, zerof=0, scenario=1)

#cross-validation to choose the tuning parameter lambda with fixed alpha=1
cv = cv_tfCox(dat, ord=0, alpha=1, n.fold=2)
#summarize the cross-validation
summary(cv)
#plot the cross-validation curve
plot(cv)
```

---

|               |                               |
|---------------|-------------------------------|
| summary.tfCox | <i>Summarize tfCox object</i> |
|---------------|-------------------------------|

---

**Description**

This function summarizes tfCox object

**Usage**

```
## S3 method for class 'tfCox'
summary(object, ...)
```

**Arguments**

|        |                                                                        |
|--------|------------------------------------------------------------------------|
| object | an object of class "tfCox"                                             |
| ...    | additional arguments to be passed. These are ignored in this function. |

**Details**

Summarize the fit by the number of knots and percent sparsity achieved. Percent sparsity is the percentage of features estimated to have no relationship with the outcome.

**Author(s)**

Jiacheng Wu

**See Also**

[tfCox](#), [plot.tfCox](#)

## Examples

```
#generate data
set.seed(1234)
dat = sim_dat(n=100, zero=0, scenario=1)

#fit piecewise constant for alpha=1 and a range of lambda
fit = tfCox(dat, ord=0, alpha=1)

#summarize the fit by the number of knots and percent sparsity achieved.
#Percent sparsity is the percentage of features estimated to have
#no relationship with outcome
summary(fit)
```

---

|       |                                                                                     |
|-------|-------------------------------------------------------------------------------------|
| tfCox | <i>Fit the additive trend filtering Cox model with a range of tuning parameters</i> |
|-------|-------------------------------------------------------------------------------------|

---

## Description

Fit additive trend filtering Cox model where each component function is estimated to be piecewise constant or polynomial.

## Usage

```
tfCox(dat, ord=0, alpha=1, lambda.seq=NULL, discrete=NULL, n.lambda=30,
lambda.min.ratio = 0.01, tol=1e-6, niter=1000, stepSize=25, backtracking=0)
```

## Arguments

|            |                                                                                                                                                                                                                                                                                                                                                                                                                          |
|------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| dat        | A list that contains time, status and X. time is failure or censoring time, status is failure indicator with 1 indicating failure and 0 indicating censoring, and X is n x p design matrix and may have p > n. Missing data are not allowed in time, status and X. X should be numeric.                                                                                                                                  |
| ord        | The polynomial order of the trend filtering fit; a non-negative interger (ord>= 3 is not recommended). For instance, ord=0 will produce piewise constant fit, ord=1 will produce piewise linear fit, and ord=2 will produce piewise quadratic fit.                                                                                                                                                                       |
| alpha      | The trade-off between trend filtering penalty and group lasso penalty. It must be in [0,1]. alpha=1 corresponds to the case with only trend filtering penalty to produce piecewise polynomial, and alpha=0 corresponds to the case with only group lasso penalty to produce sparsity of the functions. alpha between 0 and 1 is the tradeoff between the strength of these two penalties. For p < n, we suggest using 1. |
| lambda.seq | A vector of non-negative tuning parameters. If provided, lambda.seq should be a decreasing sequence of values since tfCox uses warm starts for speed. If lambda.seq=NULL, the default will calculate lambda.seq using lambda.min.ratio and n.lambda.                                                                                                                                                                     |

|                               |                                                                                                                                                                                                                             |
|-------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <code>discrete</code>         | A vector of covariate/feature indice that are discrete. Discrete covariates are not penalized in the model. Default NULL means that none of the covariates are discrete thus all covariates will be penalized in the model. |
| <code>n.lambda</code>         | The number of lambda values to consider and the default is 30.                                                                                                                                                              |
| <code>lambda.min.ratio</code> | Smallest value for <code>lambda.seq</code> , as a fraction of the maximum lambda value, which is the smallest value such that the penalty term is zero. The default is 0.01.                                                |
| <code>tol</code>              | Convergence criterion for estimates.                                                                                                                                                                                        |
| <code>niter</code>            | Maximum number of iterations.                                                                                                                                                                                               |
| <code>stepSize</code>         | Initial step size. Default is 25.                                                                                                                                                                                           |
| <code>backtracking</code>     | Whether backtracking should be used 1 (TRUE) or 0 (FALSE). Default is 0 (FALSE).                                                                                                                                            |

### Details

The optimization problem has the form

$$l(\theta) + \alpha\lambda \sum_{j=1}^p |D_j P_j \theta_j|_1 + (1 - \alpha)\lambda \sum_{j=1}^p |\theta_j|_2$$

where  $l$  is the loss function defined as the negative log partial likelihood divided by  $n$ , and  $\alpha$  provides a trade-off between trend filtering penalty and group lasso penalty. Covariate matrix  $X$  is not standardized before solving the optimization problem.

### Value

An object with S3 class "tfCox".

|                            |                                                                                                                                               |
|----------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------|
| <code>ord</code>           | the polynomial order of the trend filtering fit. Specified by user (or default).                                                              |
| <code>alpha</code>         | as specified by user (or default).                                                                                                            |
| <code>lambda.seq</code>    | vector of lambda values considered.                                                                                                           |
| <code>theta.list</code>    | list of estimated theta matrices of dimension $n \times p$ . Each component in the list corresponds to the fit from <code>lambda.seq</code> . |
| <code>num.knots</code>     | vector of number of knots of the estimated theta. Each component corresponds to the fit from <code>lambda.seq</code> .                        |
| <code>num.nonsparse</code> | vector of proportion of non-sparse/non-zero covariates/features. Each component corresponds to the fit from <code>lambda.seq</code> .         |
| <code>dat</code>           | as specified by user.                                                                                                                         |

### Author(s)

Jiacheng Wu

## References

Jiacheng Wu & Daniela Witten (2019) Flexible and Interpretable Models for Survival Data, Journal of Computational and Graphical Statistics, DOI: 10.1080/10618600.2019.1592758

## See Also

[summary.tfCox](#), [predict.tfCox](#), [plot.tfCox](#), [cv\\_tfCox](#)

## Examples

```
#####
#constant trend filtering (fused lasso) with adaptively chosen knots
#generate data from simulation scenario 1 with piecewise constant functions
set.seed(1234)
dat = sim_dat(n=100, zerof=0, scenario=1)

#fit piecewise constant for alpha=1 and a range of lambda
fit = tfCox(dat, ord=0, alpha=1)
summary(fit)
#plot the fit of lambda index 15 and the first predictor
plot(fit, which.lambda=15, which.predictor=1)

#cross-validation to choose the tuning parameter lambda with fixed alpha=1
cv = cv_tfCox(dat, ord=0, alpha=1, n.fold=2)
summary(cv)
cv$best.lambda
#plot the cross-validation curve
plot(cv)

#fit the model with the best tuning parameter chosen by cross-validation
one.fit = tfCox(dat, ord=0, alpha=1, lambda.seq=cv$best.lambda)
#predict theta from the fitted tfCox object
theta_hat = predict(one.fit, newX=dat$X, which.lambda=1)

#plot the fitted theta_hat (line) with the true theta (dot)
for (i in 1:4) {
  ordi = order(dat$X[,i])
  plot(dat$X[ordi,i], dat$true_theta[ordi,i],
       xlab=paste("predictor",i), ylab="theta" )
  lines(dat$X[ordi,i], theta_hat[ordi,i], type="s")
}

#####
#linear trend filtering with adaptively chosen knots
#generate data from simulation scenario 3 with piecewise linear functions
set.seed(1234)
dat = sim_dat(n=100, zerof=0, scenario=3)

#fit piecewise constant for alpha=1 and a range of lambda
fit = tfCox(dat, ord=1, alpha=1)
summary(fit)
```

```

#plot the fit of lambda index 15 and the first predictor
plot(fit, which.lambda=15, which.predictor=1)

#cross-validation to choose the tuning parameter lambda with fixed alpha=1
cv = cv_tfCox(dat, ord=1, alpha=1, n.fold=2)
summary(cv)
#plot the cross-validation curve
plot(cv)

#fit the model with the best tuning parameter chosen by cross-validation
one.fit = tfCox(dat, ord=1, alpha=1, lambda.seq=cv$best.lambda)
#predict theta from the fitted tfCox object
theta_hat = predict(one.fit, newX=dat$X, which.lambda=1)

#plot the fitted theta_hat (line) with the true theta (dot)
for (i in 1:4) {
  ordi = order(dat$X[,i])
  plot(dat$X[ordi,i], dat$true_theta[ordi,i],
       xlab=paste("predictor",i), ylab="theta" )
  lines(dat$X[ordi,i], theta_hat[ordi,i], type="l")
}

```

---

|                     |                                                                              |
|---------------------|------------------------------------------------------------------------------|
| tfCox_choose_lambda | <i>Choose the tuning parameter lambda using training and testing dataset</i> |
|---------------------|------------------------------------------------------------------------------|

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## Description

Fit additive trend filtering Cox model where each component function is estimated to be piecewise constant or polynomial. Tuning parameter is selected via training and testing dataset described in Wu and Witten (2019). Training data is used to build the model, and testing data is used for selecting tuning parameter based on log likelihood. It is a convenience function to replicate the simulation results in Wu and Witten (2019).

## Usage

```

tfCox_choose_lambda(dat, test_dat, ord = 0, alpha = 1, discrete = NULL,
lam_seq = NULL, nlambda = 30, c = NULL, tol = 1e-06, niter=1000,
stepSize=25, backtracking=0)

```

## Arguments

|     |                                                                                                                                                                                                                                                      |
|-----|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| dat | A list that contains time, status and X. time is failure or censoring time, status is censoring indicator, and X is n x p matrix and may have p > n. This is the training data that will be used for estimation for a given tuning parameter lambda. |
|-----|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|

|              |                                                                                                                                                                                                                                                                                                                                                                                                                             |
|--------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| test_dat     | Same list frame as before. This is the testing data that will be used for selecting tuning parameter based on the log likelihood fit.                                                                                                                                                                                                                                                                                       |
| ord          | The polynomial order of the trend filtering fit; a non-negative interger (ord>= 3 is not recommended). For instance, ord=0 will produce piewise constant fit, ord=1 will produce piewise linear fit, and ord=2 will produce piewise quadratic fit.                                                                                                                                                                          |
| alpha        | The trade-off between trend filtering penalty and group lasso penalty. It must be in [0,1]. alpha=1 corresponds to the case with only trend filtering penalty to produce piecewise polynomial, and alpha=0 corresponds to the case with only group lasso penalty to produce sparsity of the functions. alpha between 0 and 1 is the tradeoff between the strength of these two penalties. For $p < n$ , we suggest using 1. |
| discrete     | A vector of covariate/feature indice that are discrete. Discrete covariates are not penalized in the model. Default NULL means that none of the covariates are discrete thus all covariates will be penalized in the model.                                                                                                                                                                                                 |
| lam_seq      | The sequence of positive lambda values to consider. The default is NULL, which calculates lambda.seq using lambda.min.ratio and n.lambda. If lambda.seq is provided, it will override the default. lambda.seq should be a decreasing positive sequence of values since cv_tfCox relies on warm starts to speed up the computation.                                                                                          |
| nlambda      | The number of lambda values to consider. Default is 30.                                                                                                                                                                                                                                                                                                                                                                     |
| c            | Smallest value for lam_seq, as a fraction of the maximum lambda value, which is the smallest value such that the penalty term is zero. The default is NULL.                                                                                                                                                                                                                                                                 |
| tol          | Convergence criterion for estimates.                                                                                                                                                                                                                                                                                                                                                                                        |
| niter        | Maximum number of iterations.                                                                                                                                                                                                                                                                                                                                                                                               |
| stepSize     | Iniitial step size. Default is 25.                                                                                                                                                                                                                                                                                                                                                                                          |
| backtracking | Whether backtracking should be used 1 (TRUE) or 0 (FALSE). Default is 0 (FALSE).                                                                                                                                                                                                                                                                                                                                            |

### Value

|             |                                                                              |
|-------------|------------------------------------------------------------------------------|
| lam_seq     | Lambda sequence considered.                                                  |
| loss        | Loss based on the testing data with the same length as lambda.seq            |
| knots       | Number of knots from the training data with the same length as lambda.seq    |
| paramfit    | Mean square error between the estimated and true theta for the testing data. |
| best_lambda | The lambda that achieves the minimum loss for testing data.                  |

### Author(s)

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### References

Jiacheng Wu & Daniela Witten (2019) Flexible and Interpretable Models for Survival Data, Journal of Computational and Graphical Statistics, DOI: 10.1080/10618600.2019.1592758

**See Also**[predict\\_best\\_lambda](#), [negloglik](#)**Examples**

```
#generate training and testing data
dat = sim_dat(n=100, zeroof=0, scenario=1)
test_dat = sim_dat(n=100, zeroof=0, scenario=1)

#choose the optimal tuning parameter
cv = tfCox_choose_lambda(dat, test_dat, ord=0, alpha=1)
plot(cv$lam_seq, cv$loss)

#optimal tuning parameter
cv$best_lambda

#predict the coefficients of testing covariates from the optimal tuning parameter
#from tfCox_choose_lambda object.
theta_hat = predict_best_lambda(cv, test_dat$X)

#calculate the loss in the testing data based on the estimated coefficients theta
negloglik(test_dat, theta_hat)
```

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