

Package ‘rma.exact’

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Title Exact Confidence Intervals for Random Effects Meta-Analyses

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Description Compute an exact CI for the population mean under a random effects model. The routines implement the algorithm described in Michael, Thronton, Xie, and Tian (2017) <https://haben-michael.github.io/research/Exact_Inference_Meta.pdf>.

Depends R (>= 3.2.1)

License GPL-3

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+ .RMA.Exact

Combine confidence regions from two RMA.Exact objects

Description

Combine confidence regions from two RMA.Exact objects

Usage

```
## S3 method for class 'RMA.Exact'
rma1 + rma2
```

Arguments

rma1	the first RMA.Exact object
rma2	the second RMA.Exact object

Value

an object of class RMA.Exact

confint.RMA.Exact

Compute a confidence interval for the population mean from an RMA.Exact object

Description

A warning will be issued if the reported endpoints of the confidence interval are near the bounding box.

Usage

```
## S3 method for class 'RMA.Exact'
confint(object, parm, level = 0.05, ...)
```

Arguments

object	an object of class RMA.Exact
parm	(inherited)
level	the significance levels at which the compute the confidence intervals
...	(currently for internal use)

Value

a matrix with a row corresponding to each weight parameter `c0` stored in `rma0`, and columns containing the upper and lower interval endpoints, the population variance values at which those endpoints were obtained, etc.

Examples

```
## see ?RMA.Exact
```

<code>plot.RMA.Exact</code>	<i>Plot a confidence region given by an RMA.Exact object</i>
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Description

Plot a confidence region given by an RMA.Exact object

Usage

```
## S3 method for class 'RMA.Exact'
plot(x, ..., levels = c(0.01, 0.02, 0.05, 0.1, 0.15, 0.2),
     mfrow = c(1, dim(rma0)[3]))
```

Arguments

<code>x</code>	an object of class RMA.Exact
<code>...</code>	additional parameters passed down to <code>graphics::contour</code> (passed from there down to <code>plot.window</code>)
<code>levels</code>	the significance levels to plot
<code>mfrow</code>	the dimensions of the array of plotting windows for use when <code>rma0</code> contains regions for multiple weight parameters; defaults to a single row with as many as columns as regions contained in <code>rma0</code>

Value

undefined

Examples

```
## see ?RMA.Exact
```

rma.exact	<i>Compute an exact confidence interval for the grand mean in a normal-normal random effects meta-analysis.</i>
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Description

Compute an exact confidence interval for the grand mean in a normal-normal random effects meta-analysis.

Usage

```
rma.exact(yi, vi, c0 = 1, level = 0.05, mu.bounds = NULL,
          tau2.bounds = NULL, resolution = 100, resolution.mu = resolution,
          resolution.tau2 = resolution, Z = NULL, B = 3000, mu.alpha = 0.995,
          tau2.alpha = 0.995, plot = TRUE, test.stat = NULL, ...)
```

Arguments

yi	a vector containing the primary study measurements
vi	a vector of the same length as yi containing the variances of the of the primary study measurements contained in yi
c0	a vector containing the mixing parameters for the test statistics
level	the level of the confidence interval; set to NULL to plot a confidence region, otherwise rma.exact.fast is called using the specified level
mu.bounds	upper and lower bounds for the range of population effect values for constructing the confidence region; if NULL, value will be calculated from mu.alpha
tau2.bounds	upper and lower bounds for the range of population variance values for constructing the confidence region; if NULL, value will be calculated from tau2.alpha
resolution	resolution of the population mean and variance values within the bounding box
resolution.mu	resolution of the population mean values within the bounding box
resolution.tau2	resolution of the population variance values within the bounding box
Z	a matrix of length(yi) rows with each row consisting of standard normal samples to be used in the monte carlo estimation of the null distribution of the test statistic; if NULL, B values will be sampled per row
B	the number of monte carlo replicates per primary study observation to be used
mu.alpha	the level of the exact CI for constructing the bounds on the population mean dimension of the bounding box
tau2.alpha	the level of the exact CI for constructing the bounds on the population variance dimension of the bounding box
plot	whether to plot the confidence region (if level is not NULL) or its boundary (if level is NULL)
test.stat	(currently for internal use)
...	(currently for internal use)

Details

Computes an exact (up to monte carlo error), unconditional, non-randomized CI for the grand mean in a random effects meta-analysis assuming a normal-normal model for the primary study observations. This function implements the algorithm described in:

Michael, Thornton, Xie, and Tian (2017). Exact Inference on the Random Effects Model for Meta-Analyses with Few Studies. (Submitted.)

If the parameter "level" is not NULL (the default value is .05), this function passes the call down to `rma.exact.fast`, which computes a CI at the specified level. If "level" is set to NULL, an entire 2-dimensional grid of p-values is estimated. In the latter case, an `RMA.Exact` object is returned, which may be passed to a plot routine to plot contours of confidence regions.

Value

if "level" is not NULL, a named vector of CI endpoints; otherwise, an object of class `RMA.Exact`

See Also

[rma.exact.fast](#) for computing confidence intervals at specified levels, [plot.RMA.Exact](#), [confint.RMA.Exact](#)

Examples

```
set.seed(1)

K <- 5
c0 <- 1
mu0 <- 0
tau2 <- 12.5
vi <- (seq(1, 5, length=K))^2
yi <- rnorm(K)*sqrt(vi+tau2)+mu0
rma.exact(yi=yi,vi=vi)

## plotting a confidence region and printing CIs with an RMA.Exact object
rma0 <- rma.exact(yi=yi,vi=vi,level=NULL)
plot(rma0)
confint(rma0)

## confidence region with multiple c0 values using an RMA.Exact object
c0 <- c(0,.25,1)
tau2 <- 12.5
vi <- (seq(1, 5, length=K))^2
yi=rnorm(K)*sqrt(vi+tau2)+mu0
rma0 <- rma.exact(yi=yi,vi=vi,c0=c0,level=NULL)
plot(rma0)
confint(rma0)

## setting tau2.bound and other parameters to non-default values using an RMA.Exact object
Z <- matrix(rnorm(K*5e3),nrow=K)
B <- ncol(Z)
resolution <- 3e2
```

```

rma0 <- rma.exact(yi=yi,vi=vi,level=NULL,Z=Z,resolution=resolution,c0=c0,
tau2.bounds=c(1,120),resolution.tau2=1e3,resolution.mu=1e2)
plot(rma0)

c0 <- 1:4
rma0 <- rma.exact(yi=yi,vi=vi,level=NULL,Z=Z,resolution=resolution,c0=c0,
tau2.bounds=c(1,450),resolution.tau2=1e3,resolution.mu=1e2)
plot(rma0)
confint(rma0,level=c(.05))

```

rma.exact.fast	<i>Compute a confidence interval for the grand mean at a user-specified confidence level.</i>
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Description

Compute a confidence interval for the grand mean at a user-specified confidence level.

Usage

```

rma.exact.fast(yi, vi, c0 = 1.2 * (length(yi) < 6) + 0.6 * (length(yi) >= 6 &
length(yi) < 10) + 0.2 * (length(yi) >= 10), level = 0.05, plot = TRUE,
tau2.bounds = NULL, resolution = 100, Z = NULL, B = 3000,
tau2.alpha = 0.995)

```

Arguments

yi	vector of measurements from the primary studies
vi	vector of the variances of the measurements in yi
c0	vector of the mixing parameters for the test statistics
level	the level of the confidence interval
plot	indicator whether to plot the contour of the confidence region
tau2.bounds	upper and lower bounds for the range of population variance values for constructing the confidence region; if NULL, value will be calculated from tau2.alpha
resolution	resolution of the population variance values for constructing the confidence region
Z	a matrix of length(yi) rows with each row consisting of standard normal samples to be used in the monte carlo estimation of the null distribution of the test statistic; if NULL, B values will be sampled per row
B	the number of monte carlo replicates per primary study observation to be used
tau2.alpha	the level of the exact CI with which to bounds on population variance when constructing the confidence region

Value

a matrix with `length(c0)` rows and each row containing the lower and upper endpoints of the confidence interval for the given mixing parameter

See Also

[rma.exact](#) for computing entire confidence regions

Examples

```
K <- 5
c0 <- 1
mu0 <- 0
tau2 <- 12.5
vi <- (seq(1, 5, length=K))^2
yi=rnorm(K)*sqrt(vi+tau2)+mu0
rma.exact.fast(yi=yi,vi=vi,level=.05)
```

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