

Package ‘rTensor’

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Type Package

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Description A set of tools for creation, manipulation, and modeling of tensors with arbitrary number of modes. A tensor in the context of data analysis is a multidimensional array. rTensor does this by providing a S4 class 'Tensor' that wraps around the base 'array' class. rTensor provides common tensor operations as methods, including matrix unfolding, summing/averaging across modes, calculating the Frobenius norm, and taking the inner product between two tensors. Familiar array operations are overloaded, such as index subsetting via '[' and element-wise operations. rTensor also implements various tensor decomposition, including CP, GLRAM, MPCA, PVD, and Tucker. For tensors with 3 modes, rTensor also implements transpose, t-product, and t-SVD, as defined in Kilmer et al. (2013). Some auxiliary functions include the Khatri-Rao product, Kronecker product, and the Hadamard product for a list of matrices.

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Description

This package is centered around the [Tensor-class](#), which defines a S4 class for tensors of arbitrary number of modes. A vignette and/or a possible paper will be included in a future release of this package.

Details

This page will summarize the full functionality of this package. Note that since all the methods associated with S4 class [Tensor-class](#) are documented there, we will not duplicate it here.

The remaining functions can be split into two groups: the first is a set of tensor decompositions, and the second is a set of helper functions that are useful in tensor manipulation.

rTensor implements the following tensor decompositions:

[cp](#) Canonical Polyadic (CP) decomposition

[tucker](#) General Tucker decomposition

[mpca](#) Multilinear Principal Component Analysis; note that for 3-Tensors this is also known as Generalized Low Rank Approximation of Matrices(GLRAM)

[hosvd](#) (Truncated-)Higher-order singular value decomposition

[t_svd](#) Tensor singular value decomposition; 3-Tensors only; also note that there is an associated reconstruction function [t_svd_reconstruct](#)

[pvd](#) Population value decomposition of images; 3-Tensors only

rTensor also provides a set functions for tensors multiplication:

[ttm](#) Tensor times matrix, aka m-mode product

[ttl](#) Tensor times list (of matrices)

[t_mult](#) Tensor product based on block circulant unfolding; only implemented for a pair of 3-Tensors

...as well as for matrices:

[hadamard_list](#) Computes the Hadamard (element-wise) product of a list of matrices

[kronecker_list](#) Computes the Kronecker product of a list of matrices

[khatrao](#) Computes the Khatri-Rao product of two matrices

[khatrao_list](#) Computes the Khatri-Rao product of a list of matrices

[fold](#) General folding of a matrix into a tensor

[k_fold](#) Inverse operation for [k_unfold](#)

[unmatvec](#) Inverse operation for [matvec](#)

For more information on any of the functions, please consult the individual man pages.

Author(s)

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as.tensor

Tensor Conversion

Description

Create a [Tensor-class](#) object from an array, matrix, or vector.

Usage

```
as.tensor(x, drop = FALSE)
```

Arguments

x	an instance of array, matrix, or vector
drop	whether or not modes of 1 should be dropped

Value

a [Tensor-class](#) object

Examples

```
#From vector
vec <- runif(3); vecT <- as.tensor(vec); vecT
#From matrix
mat <- matrix(runif(2*3),nrow=2,ncol=3)
matT <- as.tensor(mat); matT
#From array
indices <- c(2,3,4)
arr <- array(runif(prod(indices)), dim = indices)
arrT <- as.tensor(arr); arrT
```

cp

Canonical Polyadic Decomposition

Description

Canonical Polyadic (CP) decomposition of a tensor, aka CANDECOMP/PARAFAC. Approximate a K-Tensor using a sum of num_components rank-1 K-Tensors. A rank-1 K-Tensor can be written as an outer product of K vectors. There are a total of num_components * tnsr@num_modes vectors in the output, stored in tnsr@num_modes matrices, each with num_components columns. This is an iterative algorithm, with two possible stopping conditions: either relative error in Frobenius norm has gotten below tol, or the max_iter number of iterations has been reached. For more details on CP decomposition, consult Kolda and Bader (2009).

Usage

```
cp(tnsr, num_components = NULL, max_iter = 25, tol = 1e-05)
```

Arguments

<code>tnsr</code>	Tensor with K modes
<code>num_components</code>	the number of rank-1 K-Tensors to use in approximation
<code>max_iter</code>	maximum number of iterations if error stays above <code>tol</code>
<code>tol</code>	relative Frobenius norm error tolerance

Details

Uses the Alternating Least Squares (ALS) estimation procedure. A progress bar is included to help monitor operations on large tensors.

Value

a list containing the following

- `lambdas` a vector of normalizing constants, one for each component
- `U` a list of matrices - one for each mode - each matrix with `num_components` columns
- `conv` whether or not `resid < tol` by the last iteration
- `norm_percent` the percent of Frobenius norm explained by the approximation
- `est` estimate of `tnsr` after compression
- `fnorm_resid` the Frobenius norm of the error `fnorm(est-tnsr)`
- `all_resids` vector containing the Frobenius norm of error for all the iterations

References

T. Kolda, B. Bader, "Tensor decomposition and applications". SIAM Applied Mathematics and Applications 2009.

See Also

[tucker](#)

Examples

```
### How to retrieve faces_tnsr from figshare
# faces_tnsr <- load_orl()
# subject <- faces_tnsr[, , 14, ]
dummy_faces_tnsr <- rand_tensor(c(92, 112, 40, 10))
subject <- dummy_faces_tnsr[, , 14, ]
cpD <- cp(subject, num_components=3)
cpD$conv
cpD$norm_percent
plot(cpD$all_resids)
```

cs_fold	<i>Column Space Folding of Matrix</i>
---------	---------------------------------------

Description

DEPRECATED. Please see [unmatvec](#)

Usage

```
cs_fold(mat, m = NULL, modes = NULL)
```

Arguments

- | | |
|-------|-------------------------------------|
| mat | matrix to be folded |
| m | the mode corresponding to cs_unfold |
| modes | the original modes of the tensor |

cs_unfold-methods	<i>Tensor Column Space Unfolding</i>
-------------------	--------------------------------------

Description

DEPRECATED. Please see [matvec-methods](#) and [unfold-methods](#).

Usage

```
cs_unfold(tnsr, m)

## S4 method for signature 'Tensor'
cs_unfold(tnsr, m = NULL)
```

Arguments

- | | |
|------|------------------------|
| tnsr | Tensor instance |
| m | mode to be unfolded on |

Details

```
cs_unfold(tnsr,m=NULL)
```

dim-methods*Mode Getter for Tensor*

Description

Return the vector of modes from a tensor

Usage

```
## S4 method for signature 'Tensor'
dim(x)
```

Arguments

x the Tensor instance

Details

dim(x)

Value

an integer vector of the modes associated with x

Examples

```
tnsr <- rand_tensor()
dim(tnsr)
```

fnorm-methods*Tensor Frobenius Norm*

Description

Returns the Frobenius norm of the Tensor instance.

Usage

```
fnorm(tnsr)

## S4 method for signature 'Tensor'
fnorm(tnsr)
```

Arguments

tnsr the Tensor instance

Details

```
fnorm(tnsr)
```

Value

numeric Frobenius norm of x

Examples

```
tnsr <- rand_tensor()
fnorm(tnsr)
```

fold

General Folding of Matrix

Description

General folding of a matrix into a Tensor. This is designed to be the inverse function to [unfold-methods](#), with the same ordering of the indices. This amounts to following: if we were to unfold a Tensor using a set of `row_idx` and `col_idx`, then we can fold the resulting matrix back into the original Tensor using the same `row_idx` and `col_idx`.

Usage

```
fold(mat, row_idx = NULL, col_idx = NULL, modes = NULL)
```

Arguments

<code>mat</code>	matrix to be folded into a Tensor
<code>row_idx</code>	the indices of the modes that are mapped onto the row space
<code>col_idx</code>	the indices of the modes that are mapped onto the column space
<code>modes</code>	the modes of the output Tensor

Details

This function uses `aperm` as the primary workhorse.

Value

Tensor object with modes given by `modes`

References

T. Kolda, B. Bader, "Tensor decomposition and applications". SIAM Applied Mathematics and Applications 2009.

See Also

[unfold-methods](#), [k_fold](#), [unmatvec](#)

Examples

```
tnsr <- new("Tensor", 3L, c(3L, 4L, 5L), data = runif(60))
matT3 <- unfold(tnsr, row_idx = 2, col_idx = c(3, 1))
identical(fold(matT3, row_idx = 2, col_idx = c(3, 1), modes = c(3, 4, 5)), tnsr)
```

hadamard_list

List hadamard Product

Description

Returns the hadamard (element-wise) product from a list of matrices or vectors. Commonly used for n-mode products and various Tensor decompositions.

Usage

```
hadamard_list(L)
```

Arguments

L list of matrices or vectors

Value

matrix that is the hadamard product

Note

The modes/dimensions of each element in the list must match.

See Also

[kronecker_list](#), [khatri_rao_list](#)

Examples

```
l1zt <- list('mat1' = matrix(runif(40), ncol = 4),
            'mat2' = matrix(runif(40), ncol = 4),
            'mat3' = matrix(runif(40), ncol = 4))
dim(hadamard_list(l1zt))
```

head-methods

Head for Tensor

Description

Extend head for Tensor

Usage

```
## S4 method for signature 'Tensor'
head(x, ...)
```

Arguments

x the Tensor instance
 ... additional parameters to be passed into head()

Details

head(x, ...)

See Also

[tail-methods](#)

Examples

```
tnsr <- rand_tensor()
head(tnsr)
```

hosvd

(Truncated-)Higher-order SVD

Description

Higher-order SVD of a K-Tensor. Write the K-Tensor as a (m-mode) product of a core Tensor (possibly smaller modes) and K orthogonal factor matrices. Truncations can be specified via ranks (making them smaller than the original modes of the K-Tensor will result in a truncation). For the mathematical details on HOSVD, consult Lathauwer et. al. (2000).

Usage

```
hosvd(tnsr, ranks = NULL)
```

Arguments

<code>tnsr</code>	Tensor with K modes
<code>ranks</code>	a vector of desired modes in the output core tensor, default is <code>tnsr@modes</code>

Details

A progress bar is included to help monitor operations on large tensors.

Value

a list containing the following:

`Z` core tensor with modes specified by `ranks`

`U` a list of orthogonal matrices, one for each mode

`est` estimate of `tnsr` after compression

`fnorm_resid` the Frobenius norm of the error `fnorm(est-tnsr)` - if there was no truncation, then this is on the order of `mach_eps * fnorm`.

Note

The length of `ranks` must match `tnsr@num_modes`.

References

L. Lathauwer, B.Moor, J. Vanderwalle "A multilinear singular value decomposition". Journal of Matrix Analysis and Applications 2000.

See Also

[tucker](#)

Examples

```
tnsr <- rand_tensor(c(6,7,8))
hosvdD <- hosvd(tnsr)
plot(hosvdD$fnorm_resid)
hosvdD2 <- hosvd(tnsr, ranks=c(3,3,4))
plot(hosvdD2$fnorm_resid)
```

initialize-methods	<i>Initializes a Tensor instance</i>
--------------------	--------------------------------------

Description

Not designed to be called by the user. Use as `.tensor` instead.

Usage

```
## S4 method for signature 'Tensor'
initialize(.Object, num_modes = NULL, modes = NULL,
  data = NULL)
```

Arguments

<code>.Object</code>	the tensor object
<code>num_modes</code>	number of modes of the tensor
<code>modes</code>	modes of the tensor
<code>data</code>	can be vector, matrix, or array

See Also

as.tensor

innerProd-methods	<i>Tensors Inner Product</i>
-------------------	------------------------------

Description

Returns the inner product between two Tensors

Usage

```
innerProd(tnsr1, tnsr2)

## S4 method for signature 'Tensor,Tensor'
innerProd(tnsr1, tnsr2)
```

Arguments

<code>tnsr1</code>	first Tensor instance
<code>tnsr2</code>	second Tensor instance

Details

```
innerProd(tnsr1, tnsr2)
```

Value

inner product between x1 and x2

Examples

```
tnsr1 <- rand_tensor()
tnsr2 <- rand_tensor()
innerProd(tnsr1,tnsr2)
```

khatri_rao

Khatri-Rao Product

Description

Returns the Khatri-Rao (column-wise Kronecker) product of two matrices. If the inputs are vectors then this is the same as the Kronecker product.

Usage

```
khatri_rao(x, y)
```

Arguments

x	first matrix
y	second matrix

Value

matrix that is the Khatri-Rao product

Note

The number of columns must match in the two inputs.

See Also

[kronecker](#), [khatri_rao_list](#)

Examples

```
dim(khatri_rao(matrix(runif(12),ncol=4),matrix(runif(12),ncol=4)))
```

khatri_rao_list	<i>List Khatri-Rao Product</i>
-----------------	--------------------------------

Description

Returns the Khatri-Rao product from a list of matrices or vectors. Commonly used for n-mode products and various Tensor decompositions.

Usage

```
khatri_rao_list(L, reverse = FALSE)
```

Arguments

L	list of matrices or vectors
reverse	whether or not to reverse the order

Value

matrix that is the Khatri-Rao product

Note

The number of columns must match in every element of the input list.

See Also

[khatri_rao](#)

Examples

```
smalllist <- list('mat1' = matrix(runif(12),ncol=4),
  'mat2' = matrix(runif(12),ncol=4),
  'mat3' = matrix(runif(12),ncol=4))
dim(khatri_rao_list(smalllist))
```

kronecker_list	<i>List Kronecker Product</i>
----------------	-------------------------------

Description

Returns the Kronecker product from a list of matrices or vectors. Commonly used for n-mode products and various Tensor decompositions.

Usage

```
kronecker_list(L)
```

Arguments

L list of matrices or vectors

Value

matrix that is the Kronecker product

See Also

[hadamard_list](#), [khatri_rao_list](#), [kronecker](#)

Examples

```
smalllzt <- list('mat1' = matrix(runif(12),ncol=4),
  'mat2' = matrix(runif(12),ncol=4),
  'mat3' = matrix(runif(12),ncol=4))
dim(kronecker_list(smalllzt))
```

k_fold	<i>k-mode Folding of Matrix</i>
--------	---------------------------------

Description

k-mode folding of a matrix into a Tensor. This is the inverse funtion to k_unfold in the m mode. In particular, k_fold(k_unfold(tnsr, m),m,getModes(tnsr)) will result in the original Tensor.

Usage

```
k_fold(mat, m = NULL, modes = NULL)
```

Arguments

mat matrix to be folded into a Tensor
 m the index of the mode that is mapped onto the row indices
 modes the modes of the output Tensor

Details

This is a wrapper function to [fold](#).

Value

Tensor object with modes given by modes

References

T. Kolda, B. Bader, "Tensor decomposition and applications". SIAM Applied Mathematics and Applications 2009.

See Also

[k_unfold-methods](#), [fold](#), [unmatvec](#)

Examples

```
tnsr <- new("Tensor", 3L, c(3L, 4L, 5L), data = runif(60))
matT2 <- k_unfold(tnsr, m = 2)
identical(k_fold(matT2, m = 2, modes = c(3, 4, 5)), tnsr)
```

k_unfold-methods

Tensor k-mode Unfolding

Description

Unfolding of a tensor by mapping the k th mode (specified through parameter m), and all other modes onto the column space. This is the most common type of unfolding operation for Tucker decompositions and its variants. Also known as k -mode matricization.

Usage

```
k_unfold(tnsr, m)

## S4 method for signature 'Tensor'
k_unfold(tnsr, m = NULL)
```

Arguments

tnsr	the Tensor instance
m	the index of the mode to unfold on

Details

```
k_unfold(tnsr, m = NULL)
```

Value

matrix with $x@modes[m]$ rows and $prod(x@modes[-m])$ columns

References

T. Kolda and B. Bader, "Tensor decomposition and applications". SIAM Applied Mathematics and Applications 2009.

See Also

[matvec-methods](#) and [unfold-methods](#)

Examples

```
tnsr <- rand_tensor()
matT2<-rs_unfold(tnsr,m=2)
```

load_orl	<i>ORL Database of Faces</i>
----------	------------------------------

Description

A dataset containing pictures of 40 individuals under 10 different lightings. Each image has 92 x 112 pixels. Structured as a 4-tensor with modes 92 x 112 x 40 x 10. The data is now stored in figshare <https://ndownloader.figshare.com/files/28005669>

Usage

```
load_orl()
```

Format

A Tensor object with modes 92 x 112 x 40 x 10. The first two modes correspond to the image pixels, the third mode corresponds to the individual, and the last mode corresponds to the lighting.

Source

<https://www.kaggle.com/kasikrit/att-database-of-faces>

References

AT&T Laboratories Cambridge. <https://www.kaggle.com/kasikrit/att-database-of-faces>

F. Samaria, A. Harter, "Parameterisation of a Stochastic Model for Human Face Identification". IEEE Workshop on Applications of Computer Vision 1994.

See Also

[plot_orl](#)

`matvec-methods`*Tensor Matvec Unfolding*

Description

For 3-tensors only. Stacks the slices along the third mode. This is the prevalent unfolding for T-SVD and T-MULT based on block circulant matrices.

Usage

```
matvec(tnsr)

## S4 method for signature 'Tensor'
matvec(tnsr)
```

Arguments

`tnsr` the Tensor instance

Details

```
matvec(tnsr)
```

Value

matrix with `prod(x@modes[-m])` rows and `x@modes[m]` columns

References

M. Kilmer, K. Braman, N. Hao, and R. Hoover, "Third-order tensors as operators on matrices: a theoretical and computational framework with applications in imaging". SIAM Journal on Matrix Analysis and Applications 2013.

See Also

[k_unfold-methods](#) and [unfold-methods](#)

Examples

```
tnsr <- rand_tensor(c(2,3,4))
matT1<- matvec(tnsr)
```

modeMean-methods	<i>Tensor Mean Across Single Mode</i>
------------------	---------------------------------------

Description

Given a mode for a K-tensor, this returns the K-1 tensor resulting from taking the mean across that particular mode.

Usage

```
modeMean(tnsr, m, drop)

## S4 method for signature 'Tensor'
modeMean(tnsr, m = NULL, drop = FALSE)
```

Arguments

tnsr	the Tensor instance
m	the index of the mode to average across
drop	whether or not mode m should be dropped

Details

```
modeMean(tnsr,m=NULL,drop=FALSE)
```

Value

K-1 or K Tensor, where $K = x@num_modes$

See Also

[modeSum](#)

Examples

```
tnsr <- rand_tensor()
modeMean(tnsr,1,drop=TRUE)
```

Description

Given a mode for a K-tensor, this returns the K-1 tensor resulting from summing across that particular mode.

Usage

```
modeSum(tnsr, m, drop)

## S4 method for signature 'Tensor'
modeSum(tnsr, m = NULL, drop = FALSE)
```

Arguments

tnsr	the Tensor instance
m	the index of the mode to sum across
drop	whether or not mode m should be dropped

Details

```
modeSum(tnsr,m=NULL,drop=FALSE)
```

Value

K-1 or K tensor, where $K = x@num_modes$

See Also

[modeMean](#)

Examples

```
tnsr <- rand_tensor()
modeSum(tnsr,3,drop=TRUE)
```

Description

This is basically the Tucker decomposition of a K-Tensor, [tucker](#), with one of the modes uncompressed. If $K = 3$, then this is also known as the Generalized Low Rank Approximation of Matrices (GLRAM). This implementation assumes that the last mode is the measurement mode and hence uncompressed. This is an iterative algorithm, with two possible stopping conditions: either relative error in Frobenius norm has gotten below `tol`, or the `max_iter` number of iterations has been reached. For more details on the MPCA of tensors, consult Lu et al. (2008).

Usage

```
mpca(tnsr, ranks = NULL, max_iter = 25, tol = 1e-05)
```

Arguments

<code>tnsr</code>	Tensor with K modes
<code>ranks</code>	a vector of the compressed modes of the output core Tensor, this has length K-1
<code>max_iter</code>	maximum number of iterations if error stays above <code>tol</code>
<code>tol</code>	relative Frobenius norm error tolerance

Details

Uses the Alternating Least Squares (ALS) estimation procedure. A progress bar is included to help monitor operations on large tensors.

Value

a list containing the following:

- `Z_ext` the extended core tensor, with the first K-1 modes given by `ranks`
- `U` a list of K-1 orthogonal factor matrices - one for each compressed mode, with the number of columns of the matrices given by `ranks`
- `conv` whether or not $\text{resid} < \text{tol}$ by the last iteration
- `est` estimate of `tnsr` after compression
- `norm_percent` the percent of Frobenius norm explained by the approximation
- `fnorm_resid` the Frobenius norm of the error $\text{fnorm}(\text{est} - \text{tnsr})$
- `all_resids` vector containing the Frobenius norm of error for all the iterations

Note

The length of `ranks` must match `tnsr@num_modes-1`.

References

H. Lu, K. Plataniotis, A. Venetsanopoulos, "Mpca: Multilinear principal component analysis of tensor objects". IEEE Trans. Neural networks, 2008.

See Also

[tucker](#), [hosvd](#)

Examples

```
### How to retrieve faces_tnsr from figshare
# faces_tnsr <- load_orl()
# subject <- faces_tnsr[, , 21, ]
dummy_faces_tnsr <- rand_tensor(c(92, 112, 40, 10))
subject <- dummy_faces_tnsr[, , 21, ]
mpcaD <- mpca(subject, ranks=c(10, 10))
mpcaD$conv
mpcaD$norm_percent
plot(mpcad$all_resids)
```

Ops-methods

Conformable elementwise operators for Tensor

Description

Overloads elementwise operators for tensors, arrays, and vectors that are conformable (have the same modes).

Usage

```
## S4 method for signature 'Tensor,Tensor'
Ops(e1, e2)
```

Arguments

e1	left-hand object
e2	right-hand object

Examples

```
tnsr <- rand_tensor(c(3,4,5))
tnsr2 <- rand_tensor(c(3,4,5))
tnsrsum <- tnsr + tnsr2
tnsrdiff <- tnsr - tnsr2
tnsrelemprod <- tnsr * tnsr2
tnsrelemquot <- tnsr / tnsr2
for (i in 1:3L){
  for (j in 1:4L){
```

```

for (k in 1:5L){
  stopifnot(tnsrsum@data[i,j,k]==tnsr@data[i,j,k]+tnsr2@data[i,j,k])
  stopifnot(tnsrdiff@data[i,j,k]==(tnsr@data[i,j,k]-tnsr2@data[i,j,k]))
  stopifnot(tnsrelemprod@data[i,j,k]==tnsr@data[i,j,k]*tnsr2@data[i,j,k])
  stopifnot(tnsrelemquot@data[i,j,k]==tnsr@data[i,j,k]/tnsr2@data[i,j,k])
}
}
}

```

plot_orl

*Function to plot the ORL Database of Faces***Description**

A wrapper function to image() to allow easy visualization of faces_tnsr, the ORL Face Dataset. The data is now stored in figshare <https://ndownloader.figshare.com/files/28005669>

Usage

```
plot_orl(subject = 1, condition = 1)
```

Arguments

subject	which subject to plot (1-40)
condition	which lighting condition (1-10)

References

AT&T Laboratories Cambridge. <https://www.kaggle.com/kasikrit/att-database-of-faces>
 F. Samaria, A. Harter, "Parameterisation of a Stochastic Model for Human Face Identification".
 IEEE Workshop on Applications of Computer Vision 1994.

print-methods

*Print for Tensor***Description**

Extend print for Tensor

Usage

```
## S4 method for signature 'Tensor'
print(x, ...)
```

Arguments

- x the Tensor instance
- ... additional parameters to be passed into print()

Details

print(x,...)

See Also

[show](#)

Examples

```
tnsr <- rand_tensor()
print(tnsr)
```

pvd	<i>Population Value Decomposition</i>
-----	---------------------------------------

Description

The default Population Value Decomposition (PVD) of a series of 2D images. Constructs population-level matrices P, V, and D to account for variances within as well as across the images. Structurally similar to Tucker ([tucker](#)) and GLRAM ([mpca](#)), but retains crucial differences. Requires 2*n3 + 2 parameters to specified the final ranks of P, V, and D, where n3 is the third mode (how many images are in the set). Consult Crainiceanu et al. (2013) for the construction and rationale behind the PVD model.

Usage

```
pvd(tnsr, uranks = NULL, wranks = NULL, a = NULL, b = NULL)
```

Arguments

- tnsr 3-Tensor with the third mode being the measurement mode
- uranks ranks of the U matrices
- wranks ranks of the W matrices
- a rank of $P = U \%*\% t(U)$
- b rank of $D = W \%*\% t(W)$

Details

The PVD is not an iterative method, but instead relies on n3 + 2 separate PCA decompositions. The third mode is for how many images are in the set.

Value

a list containing the following:

P population-level matrix $P = U\%*\%t(U)$, where U is constructed by stacking the truncated left eigenvectors of slicewise PCA along the third mode

V a list of image-level core matrices

D population-level matrix $D = W\%*\%t(W)$, where W is constructed by stacking the truncated right eigenvectors of slicewise PCA along the third mode

est estimate of tnsr after compression

norm_percent the percent of Frobenius norm explained by the approximation

fnorm_resid the Frobenius norm of the error `fnorm(est-tnsr)`

References

C. Crainiceanu, B. Caffo, S. Luo, V. Zipunnikov, N. Punjabi, "Population value decomposition: a framework for the analysis of image populations". Journal of the American Statistical Association, 2013.

Examples

```
### How to retrieve faces_tnsr from figshare
# faces_tnsr <- load_orl()
# subject <- faces_tnsr[, , 8, ]
dummy_faces_tnsr <- rand_tensor(c(92,112,40,10))
subject <- dummy_faces_tnsr[, , 8, ]
pvdD <- pvd(subject, uranks=rep(46,10), wranks=rep(56,10), a=46, b=56)
plot(pvdD$fnorm_resid)
```

rand_tensor	<i>Tensor with Random Entries</i>
-------------	-----------------------------------

Description

Generate a Tensor with specified modes with iid normal(0,1) entries.

Usage

```
rand_tensor(modes = c(3, 4, 5), drop = FALSE)
```

Arguments

modes the modes of the output Tensor

drop whether or not modes equal to 1 should be dropped

Value

a Tensor object with modes given by modes

Note

Default `rand_tensor()` generates a 3-Tensor with modes `c(3,4,5)`.

Examples

```
rand_tensor()  
rand_tensor(c(4,4,4))  
rand_tensor(c(10,2,1),TRUE)
```

rs_fold	<i>Row Space Folding of Matrix</i>
---------	------------------------------------

Description

DEPRECATED. Please see [k_fold](#).

Usage

```
rs_fold(mat, m = NULL, modes = NULL)
```

Arguments

mat	matrix to be folded
m	the mode corresponding to <code>rs_unfold</code>
modes	the original modes of the tensor

rs_unfold-methods	<i>Tensor Row Space Unfolding</i>
-------------------	-----------------------------------

Description

DEPRECATED. Please see [k_unfold-methods](#) and [unfold-methods](#).

Usage

```
rs_unfold(tnsr, m)  
  
## S4 method for signature 'Tensor'  
rs_unfold(tnsr, m = NULL)
```

Arguments

tnsr	Tensor instance
m	mode to be unfolded on

Details

```
rs_unfold(tnsr,m=NULL)
```

show-methods	<i>Show for Tensor</i>
--------------	------------------------

Description

Extend show for Tensor

Usage

```
## S4 method for signature 'Tensor'
show(object)
```

Arguments

object the Tensor instance

Details

```
show(object)
```

See Also

```
print
```

Examples

```
tnsr <- rand_tensor()
tnsr
```

t-methods	<i>Tensor Transpose</i>
-----------	-------------------------

Description

Implements the tensor transpose based on block circulant matrices (Kilmer et al. 2013) for 3-tensors.

Usage

```
## S4 method for signature 'Tensor'
t(x)
```

Arguments

x a 3-tensor

Details

`t(x)`

Value

tensor transpose of `x`

References

M. Kilmer, K. Braman, N. Hao, and R. Hoover, "Third-order tensors as operators on matrices: a theoretical and computational framework with applications in imaging". *SIAM Journal on Matrix Analysis and Applications* 2013.

Examples

```
tnsr <- rand_tensor()
identical(t(tnsr@data[, , 1], t(tnsr@data[, , 1]))
identical(t(tnsr@data[, , 2], t(tnsr@data[, , 5]))
identical(t(t(tnsr)), tnsr)
```

tail-methods

Tail for Tensor

Description

Extend tail for Tensor

Usage

```
## S4 method for signature 'Tensor'
tail(x, ...)
```

Arguments

<code>x</code>	the Tensor instance
<code>...</code>	additional parameters to be passed into <code>tail()</code>

Details

`tail(x, ...)`

See Also

[head-methods](#)

Examples

```
tnsr <- rand_tensor()
tail(tnsr)
```

Tensor-class

S4 Class for a Tensor

Description

An S4 class for a tensor with arbitrary number of modes. The Tensor class extends the base 'array' class to include additional tensor manipulation (folding, unfolding, reshaping, subsetting) as well as a formal class definition that enables more explicit tensor algebra.

Details

This can be seen as a wrapper class to the base array class. While it is possible to create an instance using `new`, it is also possible to do so by passing the data into `as.tensor`.

Each slot of a Tensor instance can be obtained using `@`.

The following methods are overloaded for the Tensor class: `dim-methods`, `head-methods`, `tail-methods`, `print-methods`, `show-methods`, element-wise array operations, array subsetting (extract via '['), array subset replacing (replace via '['<-'), and `tperm-methods`, which is a wrapper around the base `aperm` method.

To sum across any one mode of a tensor, use the function `modeSum-methods`. To compute the mean across any one mode, use `modeMean-methods`.

You can always unfold any Tensor into a matrix, and the `unfold-methods`, `k_unfold-methods`, and `matvec-methods` methods are for that purpose. The output can be kept as a Tensor with 2 modes or a matrix object. The vectorization function is also provided as `vec`. See the attached vignette for a visualization of the different unfoldings.

Conversion from array/matrix to Tensor is facilitated via `as.tensor`. To convert from a Tensor instance, simply invoke `@data`.

The Frobenius norm of the Tensor is given by `fnorm-methods`, while the inner product between two Tensors (of equal modes) is given by `innerProd-methods`. You can also sum through any one mode to obtain the K-1 Tensor sum using `modeSum-methods`. `modeMean-methods` provides similar functionality to obtain the K-1 Tensor mean. These are primarily meant to be used internally but may be useful in doing statistics with Tensors.

For Tensors with 3 modes, we also overloaded `t` (transpose) defined by Kilmer et.al (2013). See `t-methods`.

To create a Tensor with i.i.d. random normal(0, 1) entries, see `rand_tensor`.

Slots

num_modes number of modes (integer)

modes vector of modes (integer), aka sizes/extents/dimensions

data actual data of the tensor, which can be 'array' or 'vector'

Methods

```

[ signature(tnsr = "Tensor"): ...
[<- signature(tnsr = "Tensor"): ...
matvec signature(tnsr = "Tensor"): ...
dim signature(tnsr = "Tensor"): ...
fnorm signature(tnsr = "Tensor"): ...
head signature(tnsr = "Tensor"): ...
initialize signature(.Object = "Tensor"): ...
innerProd signature(tnsr1 = "Tensor", tnsr2 = "Tensor"): ...
modeMean signature(tnsr = "Tensor"): ...
modeSum signature(tnsr = "Tensor"): ...
Ops signature(e1 = "array", e2 = "Tensor"): ...
Ops signature(e1 = "numeric", e2 = "Tensor"): ...
Ops signature(e1 = "Tensor", e2 = "array"): ...
Ops signature(e1 = "Tensor", e2 = "numeric"): ...
Ops signature(e1 = "Tensor", e2 = "Tensor"): ...
print signature(tnsr = "Tensor"): ...
k_unfold signature(tnsr = "Tensor"): ...
show signature(tnsr = "Tensor"): ...
t signature(tnsr = "Tensor"): ...
tail signature(tnsr = "Tensor"): ...
unfold signature(tnsr = "Tensor"): ...
tperm signature(tnsr = "Tensor"): ...
image signature(tnsr = "Tensor"): ...

```

Note

All of the decompositions and regression models in this package require a Tensor input.

Author(s)

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References

James Li, Jacob Bien, Martin T. Wells (2018). rTensor: An R Package for Multidimensional Array (Tensor) Unfolding, Multiplication, and Decomposition. *Journal of Statistical Software*, 87(10), 1-31. URL <http://www.jstatsoft.org/v087/i10/>.

See Also

[as.tensor](#)

Examples

```
tnsr <- rand_tensor()
class(tnsr)
tnsr
print(tnsr)
dim(tnsr)
tnsr@num_modes
tnsr@data
```

tperm-methods

Mode Permutation for Tensor

Description

Overloads aperm for Tensor class for convenience.

Usage

```
tperm(tnsr, perm, ...)

## S4 method for signature 'Tensor'
tperm(tnsr, perm, ...)
```

Arguments

tnsr	the Tensor instance
perm	the new permutation of the current modes
...	additional parameters to be passed into aperm

Details

```
tperm(tnsr, perm=NULL, ...)
```

Examples

```
tnsr <- rand_tensor(c(3,4,5))
dim(tperm(tnsr, perm=c(2,1,3)))
dim(tperm(tnsr, perm=c(1,3,2)))
```

ttl

*Tensor Times List***Description**

Contracted (m-Mode) product between a Tensor of arbitrary number of modes and a list of matrices. The result is folded back into Tensor.

Usage

```
ttl(tnsr, list_mat, ms = NULL)
```

Arguments

<code>tnsr</code>	Tensor object with K modes
<code>list_mat</code>	a list of matrices
<code>ms</code>	a vector of modes to contract on (order should match the order of <code>list_mat</code>)

Details

Performs `ttm` repeated for a single Tensor and a list of matrices on multiple modes. For instance, suppose we want to do multiply a Tensor object `tnsr` with three matrices `mat1`, `mat2`, `mat3` on modes 1, 2, and 3. We could do `ttm(ttm(ttm(tnsr, mat1, 1), mat2, 2), 3)`, or we could do `ttl(tnsr, list(mat1, mat2, mat3), c(1, 2, 3))`. The order of the matrices in the list should obviously match the order of the modes. This is a common operation for various Tensor decompositions such as CP and Tucker. For the math on the m-Mode Product, see Kolda and Bader (2009).

Value

Tensor object with K modes

Note

The returned Tensor does not drop any modes equal to 1.

References

T. Kolda, B. Bader, "Tensor decomposition and applications". SIAM Applied Mathematics and Applications 2009.

See Also

[ttm](#)

Examples

```
tnsr <- new("Tensor",3L,c(3L,4L,5L),data=runif(60))
lzt <- list('mat1' = matrix(runif(30),ncol=3),
'mat2' = matrix(runif(40),ncol=4),
'mat3' = matrix(runif(50),ncol=5))
ttl(tnsr,lzt,ms=c(1,2,3))
```

ttm	<i>Tensor Times Matrix (m-Mode Product)</i>
-----	---

Description

Contracted (m-Mode) product between a Tensor of arbitrary number of modes and a matrix. The result is folded back into Tensor.

Usage

```
ttm(tnsr, mat, m = NULL)
```

Arguments

tnsr	Tensor object with K modes
mat	input matrix with same number columns as the mth mode of tnsr
m	the mode to contract on

Details

By definition, $\text{rs_unfold}(\text{ttm}(\text{tnsr}, \text{mat}), m) = \text{mat} \% \% \text{rs_unfold}(\text{tnsr}, m)$, so the number of columns in mat must match the mth mode of tnsr. For the math on the m-Mode Product, see Kolda and Bader (2009).

Value

a Tensor object with K modes

Note

The mth mode of tnsr must match the number of columns in mat. By default, the returned Tensor does not drop any modes equal to 1.

References

T. Kolda, B. Bader, "Tensor decomposition and applications". SIAM Applied Mathematics and Applications 2009.

See Also

[ttl](#), [rs_unfold-methods](#)

Examples

```
tnsr <- new("Tensor", 3L, c(3L, 4L, 5L), data = runif(60))
mat <- matrix(runif(50), ncol = 5)
ttm(tnsr, mat, m = 3)
```

tucker

Tucker Decomposition

Description

The Tucker decomposition of a tensor. Approximates a K-Tensor using a n-mode product of a core tensor (with modes specified by ranks) with orthogonal factor matrices. If there is no truncation in one of the modes, then this is the same as the MPCA, [mpca](#). If there is no truncation in all the modes (i.e. `ranks = tnsr@modes`), then this is the same as the HOSVD, [hosvd](#). This is an iterative algorithm, with two possible stopping conditions: either relative error in Frobenius norm has gotten below `tol`, or the `max_iter` number of iterations has been reached. For more details on the Tucker decomposition, consult Kolda and Bader (2009).

Usage

```
tucker(tnsr, ranks = NULL, max_iter = 25, tol = 1e-05)
```

Arguments

<code>tnsr</code>	Tensor with K modes
<code>ranks</code>	a vector of the modes of the output core Tensor
<code>max_iter</code>	maximum number of iterations if error stays above <code>tol</code>
<code>tol</code>	relative Frobenius norm error tolerance

Details

Uses the Alternating Least Squares (ALS) estimation procedure also known as Higher-Order Orthogonal Iteration (HOOI). Initialized using a (Truncated-)HOSVD. A progress bar is included to help monitor operations on large tensors.

Value

a list containing the following:

- `Z` the core tensor, with modes specified by `ranks`
- `U` a list of orthogonal factor matrices - one for each mode, with the number of columns of the matrices given by `ranks`
- `conv` whether or not `resid < tol` by the last iteration
- `est` estimate of `tnsr` after compression
- `norm_percent` the percent of Frobenius norm explained by the approximation
- `fnorm_resid` the Frobenius norm of the error `fnorm(est - tnsr)`
- `all_resids` vector containing the Frobenius norm of error for all the iterations

Note

The length of ranks must match `tnsr@num_modes`.

References

T. Kolda, B. Bader, "Tensor decomposition and applications". SIAM Applied Mathematics and Applications 2009.

See Also

[hosvd](#), [mpca](#)

Examples

```
tnsr <- rand_tensor(c(4,4,4,4))
tuckerD <- tucker(tnsr,ranks=c(2,2,2,2))
tuckerD$conv
tuckerD$norm_percent
plot(tuckerD$all_resids)
```

t_mult

Tensor Multiplication (T-MULT)

Description

Implements T-MULT based on block circulant matrices (Kilmer et al. 2013) for 3-tensors.

Usage

```
t_mult(x, y)
```

Arguments

x	a 3-tensor
y	another 3-tensor

Details

Uses the Fast Fourier Transform (FFT) speed up suggested by Kilmer et al. 2013 instead of explicitly constructing the block circulant matrix. For the mathematical details of T-MULT, see Kilmer et al. (2013).

Value

tensor product between x and y

Note

This only works (so far) between 3-Tensors.

References

M. Kilmer, K. Braman, N. Hao, and R. Hoover, "Third-order tensors as operators on matrices: a theoretical and computational framework with applications in imaging". SIAM Journal on Matrix Analysis and Applications 2013.

Examples

```
tnsr <- new("Tensor", 3L, c(3L, 4L, 5L), data = runif(60))
tnsr2 <- new("Tensor", 3L, c(4L, 3L, 5L), data = runif(60))
t_mult(tnsr, tnsr2)
```

t_svd

Tensor Singular Value Decomposition

Description

TSVD for a 3-Tensor. Constructs 3-Tensors U , S , V such that $\text{tnsr} = \text{t_mult}(\text{t_mult}(U, S), \text{t}(V))$. U and V are orthogonal 3-Tensors with orthogonality defined in Kilmer et al. (2013), and S is a 3-Tensor consists of facewise diagonal matrices. For more details on the TSVD, consult Kilmer et al. (2013).

Usage

```
t_svd(tnsr)
```

Arguments

tnsr 3-Tensor to decompose via TSVD

Value

a list containing the following:

U the left orthogonal 3-Tensor

V the right orthogonal 3-Tensor

S the middle 3-Tensor consisting of face-wise diagonal matrices

Note

Computation involves complex values, but if the inputs are real, then the outputs are also real. Some loss of precision occurs in the truncation of the imaginary components during the FFT and inverse FFT.

References

M. Kilmer, K. Braman, N. Hao, and R. Hoover, "Third-order tensors as operators on matrices: a theoretical and computational framework with applications in imaging". SIAM Journal on Matrix Analysis and Applications 2013.

See Also

[t_mult](#), [t_svd_reconstruct](#)

Examples

```
tnsr <- rand_tensor()
tsvdD <- t_svd(tnsr)
```

t_svd_reconstruct	<i>Reconstruct Tensor From TSVD</i>
-------------------	-------------------------------------

Description

Reconstruct the original 3-Tensor after it has been decomposed into U, S, V via [t_svd](#).

Usage

```
t_svd_reconstruct(L)
```

Arguments

L list that is an output from [t_svd](#)

Value

a 3-Tensor

See Also

[t_svd](#)

Examples

```
tnsr <- rand_tensor(c(10,10,10))
tsvdD <- t_svd(tnsr)
1 - fnorm(t_svd_reconstruct(tsvdD)-tnsr)/fnorm(tnsr)
```

Description

Unfolds the tensor into a matrix, with the modes in `rs` onto the rows and modes in `cs` onto the columns. Note that `c(rs,cs)` must have the same elements (order doesn't matter) as `x@modes`. Within the rows and columns, the order of the unfolding is determined by the order of the modes. This convention is consistent with Kolda and Bader (2009).

Usage

```
unfold(tnsr, row_idx, col_idx)

## S4 method for signature 'Tensor'
unfold(tnsr, row_idx = NULL, col_idx = NULL)
```

Arguments

<code>tnsr</code>	the Tensor instance
<code>row_idx</code>	the indices of the modes to map onto the row space
<code>col_idx</code>	the indices of the modes to map onto the column space

Details

For Row Space Unfolding or m-mode Unfolding, see [rs_unfold-methods](#). For Column Space Unfolding or matvec, see [cs_unfold-methods](#).

[vec-methods](#) returns the vectorization of the tensor.

```
unfold(tnsr,row_idx=NULL,col_idx=NULL)
```

Value

matrix with `prod(row_idx)` rows and `prod(col_idx)` columns

References

T. Kolda, B. Bader, "Tensor decomposition and applications". SIAM Applied Mathematics and Applications 2009.

See Also

[k_unfold-methods](#) and [matvec-methods](#)

Examples

```
tnsr <- rand_tensor()
matT3<-unfold(tnsr,row_idx=2,col_idx=c(3,1))
```

unmatvec	<i>Unmatvec Folding of Matrix</i>
----------	-----------------------------------

Description

The inverse operation to [matvec-methods](#), turning a matrix into a Tensor. For a full account of matrix folding/unfolding operations, consult Kolda and Bader (2009).

Usage

```
unmatvec(mat, modes = NULL)
```

Arguments

mat	matrix to be folded into a Tensor
modes	the modes of the output Tensor

Value

Tensor object with modes given by modes

References

T. Kolda, B. Bader, "Tensor decomposition and applications". SIAM Applied Mathematics and Applications 2009.

See Also

[matvec-methods](#), [fold](#), [k_fold](#)

Examples

```
tnsr <- new("Tensor", 3L, c(3L, 4L, 5L), data = runif(60))
matT1 <- matvec(tnsr)
identical(unmatvec(matT1, modes = c(3, 4, 5)), tnsr)
```

vec-methods

Tensor Vec

Description

Turns the tensor into a single vector, following the convention that earlier indices vary slower than later indices.

Usage

```
vec(tnsr)
```

```
## S4 method for signature 'Tensor'  
vec(tnsr)
```

Arguments

tnsr the Tensor instance

Details

```
vec(tnsr)
```

Value

vector with length `prod(x@modes)`

References

T. Kolda, B. Bader, "Tensor decomposition and applications". SIAM Applied Mathematics and Applications 2009.

Examples

```
tnsr <- rand_tensor(c(4,5,6,7))  
vec(tnsr)
```


[-methods

*Extract or Replace Subtensors***Description**

Extends '[' and '[<-' from the base array class for the Tensor class. Works exactly as it would for the base 'array' class.

Usage

```
## S4 method for signature 'Tensor'
x[i, j, ..., drop = TRUE]

## S4 replacement method for signature 'Tensor'
x[i, j, ...] <- value
```

Arguments

x	Tensor to be subset
i, j, ...	indices that specify the extents of the sub-tensor
drop	whether or not to reduce the number of modes to exclude those that have '1' as the mode
value	either vector, matrix, or array that will replace the subtensor

Details

```
x[i,j,...,drop=TRUE]
```

Value

an object of class Tensor

Examples

```
tnsr <- rand_tensor()
tnsr[1,2,3]
tnsr[3,1,]
tnsr[, ,5]
tnsr[, ,5,drop=FALSE]

tnsr[1,2,3] <- 3; tnsr[1,2,3]
tnsr[3,1,] <- rep(0,5); tnsr[3,1,]
tnsr[,2,] <- matrix(0,nrow=3,ncol=5); tnsr[,2,]
```

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