Package 'fmx'

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Description A parametrization framework for finite mixture distribution using S4 objects. Density, cumulative density, quantile and simulation functions are defined. Currently normal, Tukey g-&-h, skew-normal and skew-t distributions are well tested. The gamma, negative binomial distributions are being tested.

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`fmx-package` *Finite Mixture Parametrization*

Description

A parametrization framework for finite mixture distribution using S4 objects.

Density, cumulative density, quantile and simulation functions are defined.

Currently normal, Tukey g-&-h, skew-normal and skew-t distributions are well tested. The gamma, negative binomial distributions are being tested.

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`approxdens` *Empirical Density Function*

Description

..

Usage

```
approxdens(x, ...)
```

Arguments

x	numeric vector, observations
...	additional parameters of density.default

Details

approx inside density.default

another 'layer' of approxfun

Value

Function `approxdens()` returns a function.

Examples

```
x = rnorm(1e3L)
f = approxdens(x)
f(x[1:3])
```

---

as.fmx *Turn Various Objects to fmx Class*

Description

Turn various objects created in other R packages to fmx class.

Usage

```
as.fmx(x, ...)
```

Arguments

x	an R object
...	additional parameters, see **Arguments** in individual S3 dispatches

Details

Various mixture distribution estimates obtained from other R packages are converted to fmx class, so that we could take advantage of all methods defined for fmx objects.

Value

S3 generic function `as.fmx()` returns an fmx object.

as.fmx.fitdist *Convert fitdist Objects to fmx Class*

Description

To convert fitdist objects (from package **fitdistrplus**) to fmx class.

Usage

```
## S3 method for class 'fitdist'
as.fmx(x, ...)
```

Arguments

x	fitdist object
...	..

Value

Function `as.fmx.fitdist()` returns an fmx object.

Examples

```
library(fitdistrplus)
# ?fitdist
data(endosulfan, package = 'fitdistrplus')
ATV <- subset(endosulfan, group == 'NonArthroInvert')$ATV
log10ATV <- log10(ATV)
fln <- fitdist(log10ATV, distr = 'norm')
(fln2 <- as.fmx(fln))
hist.default(log10ATV, freq = FALSE)
curve(dfmx(x, dist = fln2), xlim = range(log10ATV), add = TRUE)
```

as.fmx.mixEM *Convert* mixEM *Objects to fmx Class*

Description

To convert `mixEM` objects (from package **mixtools**) to fmx class.

Currently only the returned value of normalmixEM and gammamixEM are supported

Usage

```
## S3 method for class 'mixEM'
as.fmx(x, data = x[["x"]], ...)
```

Arguments

x	mixEM object
data	numeric vector
...	..

Value

Function as.fmx.mixEM() returns an fmx object.

Note

plot.mixEM not plot gammamixEM returns, as of 2022-09-19.

Examples

```
library(mixtools)
(wait = as.fmx(normalmixEM(faithful$waiting, k = 2)))
hist.default(faithful$waiting, freq = FALSE)
curve(dfmx(x, dist = wait), xlim = range(faithful$waiting), add = TRUE)
```

---

as.fmx.Normal *Convert* Normal *fit from* R*hrefhttps://CRAN.R-project.org/package=mixsmsn***mixsmsn** *to fmx*

Description

To convert Normal object (from package **mixsmsn**) to fmx class.

Usage

```
## S3 method for class 'Normal'
as.fmx(x, data, ...)
```

Arguments

x	'Normal' object, returned from smsn.mix with parameter family = 'Normal'
data	numeric vector
...	additional parameters, currently not in use

Value

Function as.fmx.Normal() returns an fmx object.

Note

smsn.mix does not offer a parameter to keep the input data, as of 2021-10-06.

Examples

```
library(mixsmsn)
# ?smsn.mix
arg1 = c(mu = 5, sigma2 = 9, lambda = 5, nu = 5)
arg2 = c(mu = 20, sigma2 = 16, lambda = -3, nu = 5)
arg3 = c(mu = 35, sigma2 = 9, lambda = -6, nu = 5)
set.seed(120); x = rmix(n = 1e3L, p=c(.5, .2, .3), family = 'Skew.t',
  arg = list(unname(arg1), unname(arg2), unname(arg3)))

# Normal
class(m2 <- smsn.mix(x, nu = 3, g = 3, family = 'Normal', calc.im = FALSE))
mix.hist(y = x, model = m2)
m2a = as.fmx(m2, data = x)
hist(x, freq = FALSE)
curve(dfmx(x, dist = m2a), xlim = range(x), add = TRUE)
```

---

as.fmx.Skew.normal *Convert* Skew.normal *Object to fmx*

Description

To convert Skew.normal object (from package **mixsmsn**) to fmx class.

Usage

```
## S3 method for class 'Skew.normal'
as.fmx(x, data, ...)
```

Arguments

x	'Skew.normal' object, returned from smsn.mix with parameter family = 'Skew.normal'.
data	numeric vector
...	additional parameters, currently not in use

Value

Function as.fmx.Skew.normal() returns an fmx object.

Note

smsn.mix does not offer a parameter to keep the input data, as of 2021-10-06.

Examples

```
library(mixsmsn)
# ?smsn.mix
arg1 = c(mu = 5, sigma2 = 9, lambda = 5, nu = 5)
arg2 = c(mu = 20, sigma2 = 16, lambda = -3, nu = 5)
arg3 = c(mu = 35, sigma2 = 9, lambda = -6, nu = 5)
set.seed(120); x = rmix(n = 1e3L, p=c(.5, .2, .3), family = 'Skew.t',
  arg = list(unname(arg1), unname(arg2), unname(arg3)))

# Skew Normal
class(m1 <- smsn.mix(x, nu = 3, g = 3, family = 'Skew.normal', calc.im = FALSE))
mix.hist(y = x, model = m1)
m1a = as.fmx(m1, data = x)
(l1a = logLik(m1a))
hist(x, freq = FALSE)
curve(dfmx(x, dist = m1a), xlim = range(x), add = TRUE)
```

`as.fmx.Skew.t` *Convert* `Skew.t` *fit from* R*hrefhttps://CRAN.R-project.org/package=mixsmsn***mixsmsn** *to fmx*

Description

To convert `Skew.t` object (from package **mixsmsn**) to fmx class.

Usage

```
## S3 method for class 'Skew.t'
as.fmx(x, data, ...)
```

Arguments

`x`	`'Skew.t'` object, returned from smsn.mix with parameter `family = 'Skew.t'`
`data`	numeric vector
`...`	additional parameters, currently not in use

Value

Function `as.fmx.Skew.t()` returns an fmx object.

Note

smsn.mix does not offer a parameter to keep the input data, as of 2021-10-06.

Examples

```
# mixsmsn::smsn.mix with option `family = 'Skew.t'` is slow

library(mixsmsn)
# ?smsn.mix
arg1 = c(mu = 5, sigma2 = 9, lambda = 5, nu = 5)
arg2 = c(mu = 20, sigma2 = 16, lambda = -3, nu = 5)
arg3 = c(mu = 35, sigma2 = 9, lambda = -6, nu = 5)
set.seed(120); x = rmix(n = 1e3L, p=c(.5, .2, .3), family = 'Skew.t',
  arg = list(unname(arg1), unname(arg2), unname(arg3)))

# Skew t
class(m3 <- smsn.mix(x, nu = 3, g = 3, family = 'Skew.t', calc.im = FALSE))
mix.hist(y = x, model = m3)
m3a = as.fmx(m3, data = x)
hist(x, freq = FALSE)
curve(dfmx(x, dist = m3a), xlim = range(x), add = TRUE)
(l3a = logLik(m3a))
stopifnot(all.equal.numeric(AIC(l3a), m3$aic), all.equal.numeric(BIC(l3a), m3$bic))
```

`as.fmx.t` *Convert* `t` *fit from* R*hrefhttps://CRAN.R-project.org/package=mixsmsn***mixsmsn** *to fmx*

Description

To convert `t` object (from package **mixsmsn**) to fmx class.

Usage

```
## S3 method for class 't'
as.fmx(x, data, ...)
```

Arguments

`x`	`'t'` object, returned from smsn.mix with parameter `family = 't'`
`data`	numeric vector
`...`	additional parameters, currently not in use

Value

Function `as.fmx.t()` has not been completed yet

Note

smsn.mix does not offer a parameter to keep the input data, as of 2021-10-06.

Examples

```
library(mixsmsn)
# ?smsn.mix
arg1 = c(mu = 5, sigma2 = 9, lambda = 5, nu = 5)
arg2 = c(mu = 20, sigma2 = 16, lambda = -3, nu = 5)
arg3 = c(mu = 35, sigma2 = 9, lambda = -6, nu = 5)
set.seed(120); x = rmix(n = 1e3L, p=c(.5, .2, .3), family = 'Skew.t',
  arg = list(unname(arg1), unname(arg2), unname(arg3)))

# t
class(m4 <- smsn.mix(x, nu = 3, g = 3, family = 't', calc.im = FALSE))
mix.hist(y = x, model = m4)
# as.fmx(m4, data = x) # not ready yet!!
```

---

dfmx *Density, Distribution and Quantile of Finite Mixture Distribution*

Description

Density function, distribution function, quantile function and random generation for a finite mixture distribution with normal or Tukey g-&-h components.

Usage

```
dfmx(
  x,
  dist,
  distname = dist@distname,
  K = dim(pars)[1L],
  pars = dist@pars,
  w = dist@w,
  ...,
  log = FALSE
)

pfmx(
  q,
  dist,
  distname = dist@distname,
  K = dim(pars)[1L],
  pars = dist@pars,
  w = dist@w,
  ...,
  lower.tail = TRUE,
  log.p = FALSE
)
```

```
qfmx(
  p,
  dist,
  distname = dist@distname,
  K = dim(pars)[1L],
  pars = dist@pars,
  w = dist@w,
  interval = qfmx_interval(dist = dist),
  ...,
  lower.tail = TRUE,
  log.p = FALSE
)

rfmx(
  n,
  dist,
  distname = dist@distname,
  K = dim(pars)[1L],
  pars = dist@pars,
  w = dist@w
)
```

Arguments

x, q	numeric vector, quantiles, NA_real_ value(s) allowed.
dist	fmx object, a finite mixture distribution
distname, K, pars, w	auxiliary parameters, whose default values are determined by argument dist. The user-specified vector of w does not need to sum up to 1; w/sum(w) will be used internally.
...	additional parameters
log, log.p	logical scalar. If TRUE, probabilities are given as $\log(p)$.
lower.tail	logical scalar. If TRUE (default), probabilities are $Pr(X \leq x)$, otherwise, $Pr(X > x)$.
p	numeric vector, probabilities.
interval	length two numeric vector, interval for root finding, see vuniroot2 and vuniroot
n	integer scalar, number of observations.

Details

A computational challenge in function dfmx() is when mixture density is very close to 0, which happens when the per-component log densities are negative with big absolute values. In such case, we cannot compute the log mixture densities (i.e., -Inf), for the log-likelihood using function logLik.fmx(). Our solution is to replace these -Inf log mixture densities by the weighted average (using the mixing proportions of dist) of the per-component log densities.

Function qfmx() gives the quantile function, by numerically solving pfmx. One major challenge when dealing with the finite mixture of Tukey g-&-h family distribution is that Brent–Dekker's method needs to be performed in both pGH and qfmx functions, i.e. *two layers* of root-finding algorithm.

Value

Function dfmx() returns a numeric vector of probability density values of an fmx object at specified quantiles x.

Function pfmx() returns a numeric vector of cumulative probability values of an fmx object at specified quantiles q.

Function qfmx() returns an unnamed numeric vector of quantiles of an fmx object, based on specified cumulative probabilities p.

Function rfmx() generates random deviates of an fmx object.

Note

Function qnorm returns an unnamed vector of quantiles, although quantile returns a named vector of quantiles.

Examples

```
library(ggplot2)

(e1 = fmx('norm', mean = c(0,3), sd = c(1,1.3), w = c(1, 1)))
curve(dfmx(x, dist = e1), xlim = c(-3,7))
ggplot() + geom_function(fun = dfmx, args = list(dist = e1)) + xlim(-3,7)
ggplot() + geom_function(fun = pfmx, args = list(dist = e1)) + xlim(-3,7)
hist(rfmx(n = 1e3L, dist = e1), main = '1000 obs from e1')

x = (-3):7
round(dfmx(x, dist = e1), digits = 3L)
round(p1 <- pfmx(x, dist = e1), digits = 3L)
stopifnot(all.equal.numeric(qfmx(p1, dist = e1), x, tol = 1e-4))

(e2 = fmx('GH', A = c(0,3), g = c(.2, .3), h = c(.2, .1), w = c(2, 3)))
ggplot() + geom_function(fun = dfmx, args = list(dist = e2)) + xlim(-3,7)

round(dfmx(x, dist = e2), digits = 3L)
round(p2 <- pfmx(x, dist = e2), digits = 3L)
stopifnot(all.equal.numeric(qfmx(p2, dist = e2), x, tol = 1e-4))

(e3 = fmx('GH', g = .2, h = .01)) # one-component Tukey
ggplot() + geom_function(fun = dfmx, args = list(dist = e3)) + xlim(-3,5)
set.seed(124); r1 = rfmx(1e3L, dist = e3);
set.seed(124); r2 = TukeyGH77::rGH(n = 1e3L, g = .2, h = .01)
stopifnot(identical(r1, r2)) # but ?rfmx has much cleaner code
round(dfmx(x, dist = e3), digits = 3L)
round(p3 <- pfmx(x, dist = e3), digits = 3L)
stopifnot(all.equal.numeric(qfmx(p3, dist = e3), x, tol = 1e-4))
```

```
a1 = fmx('GH', A = c(7,9), B = c(.8, 1.2), g = c(.3, 0), h = c(0, .1), w = c(1, 1))
a2 = fmx('GH', A = c(6,9), B = c(.8, 1.2), g = c(-.3, 0), h = c(.2, .1), w = c(4, 6))
library(ggplot2)
(p = ggplot() +
 geom_function(fun = pfmx, args = list(dist = a1), mapping = aes(color = 'g2=h1=0')) +
 geom_function(fun = pfmx, args = list(dist = a2), mapping = aes(color = 'g2=0')) +
 xlim(3,15) +
 scale_y_continuous(labels = scales::percent) +
 labs(y = NULL, color = 'models') +
 coord_flip())
p + theme(legend.position = 'none')


# to use [rfmx] without \pkg{fmx}
(d = fmx(distname = 'GH', A = c(-1,1), B = c(.9,1.1), g = c(.3,-.2), h = c(.1,.05), w = c(2,3)))
d@pars
set.seed(14123); x = rfmx(n = 1e3L, dist = d)
set.seed(14123); x_raw = rfmx(n = 1e3L,
 distname = 'GH', K = 2L,
 pars = rbind(
  c(A = -1, B = .9, g = .3, h = .1),
  c(A = 1, B = 1.1, g = -.2, h = .05)
 ),
 w = c(.4, .6)
)
stopifnot(identical(x, x_raw))
```

`fmx` *Create fmx Object for Finite Mixture Distribution*

Description

To create fmx object for finite mixture distribution.

Usage

```
fmx(distname, w = 1, ...)
```

Arguments

`distname`	character scalar
`w`	(optional) numeric vector. Does not need to sum up to 1; `w/sum(w)` will be used internally.
`...`	mixture distribution parameters. See function dGH for the names and default values of Tukey g-&-h distribution parameters, or dnorm for the names and default values of normal distribution parameters.

Value

Function fmx() returns an fmx object.

Examples

```
(e1 = fmx('norm', mean = c(0,3), sd = c(1,1.3), w = c(1, 1)))
isS4(e1) # TRUE
slotNames(e1)

(e2 = fmx('GH', A = c(0,3), g = c(.2, .3), h = c(.2, .1), w = c(2, 3)))

(e3 = fmx('GH', A = 0, g = .2, h = .2)) # one-component Tukey
```

---

fmx-class *fmx Class: Finite Mixture Parametrization*

Description

An S4 object to specify the parameters and type of distribution of a one-dimensional finite mixture distribution.

Slots

`distname` character scalar, name of parametric distribution of the mixture components. Currently, normal (`'norm'`) and Tukey g-&-h (`'GH'`) distributions are supported.

`pars` double matrix, all distribution parameters in the mixture. Each row corresponds to one component. Each column includes the same parameters of all components. The order of rows corresponds to the (non-strictly) increasing order of the component location parameters. The columns match the formal arguments of the corresponding distribution, e.g., `'mean'` and `'sd'` for normal mixture, or `'A'`, `'B'`, `'g'` and `'h'` for Tukey g-&-h mixture.

`w` numeric vector of mixing proportions that must sum to 1

`data` (optional) numeric vector, the one-dimensional observations

`data.name` (optional) character scalar, a human-friendly name of the observations

`vcov_internal` (optional) variance-covariance matrix of the internal (i.e., unconstrained) estimates

`vcov` (optional) variance-covariance matrix of the mixture distribution (i.e., constrained) estimates

`Kolmogorov,CramerVonMises,KullbackLeibler` (optional) numeric scalars

`fmx_constraint` *Parameter Constraint(s) of Mixture Distribution*

Description

Determine the parameter constraint(s) of a finite mixture distribution fmx, either by the value of parameters of such mixture distribution, or by a user-specified string.

Usage

```
fmx_constraint(
  dist,
  distname = dist@distname,
  K = dim(dist@pars)[1L],
  pars = dist@pars
)
```

Arguments

`dist`	(optional) fmx object
`distname`	character scalar, name of distribution (see fmx), default value determined by `dist`
`K`	integer scalar, number of components, default value determined by `dist`
`pars`	double matrix, distribution parameters of a finite mixture distribution (see fmx), default value determined by `dist`

Value

Function `fmx_constraint()` returns the indices of internal parameters (only applicable to Tukey g-&-h mixture distribution, yet) to be constrained, based on the input fmx object `dist`.

Examples

```
(d0 = fmx('GH', A = c(1,4), g = c(.2,.1), h = c(.05,.1), w = c(1,1)))
(c0 = fmx_constraint(d0))
user_constraint(character(), distname = 'GH', K = 2L) # equivalent

(d1 = fmx('GH', A = c(1,4), g = c(.2,0), h = c(0,.1), w = c(1,1)))
(c1 = fmx_constraint(d1))
user_constraint(c('g2', 'h1'), distname = 'GH', K = 2L) # equivalent

(d2 = fmx('GH', A = c(1,4), g = c(.2,0), h = c(.15,.1), w = c(1,1)))
(c2 = fmx_constraint(d2))
user_constraint('g2', distname = 'GH', K = 2L) # equivalent
```

`Kolmogorov_dist` *One-Sample Kolmogorov Distance*

Description

To calculate the one-sample Kolmogorov distance between observations and a distribution.

Usage

```
Kolmogorov_dist(x, null, alternative = c("two.sided", "less", "greater"), ...)
```

Arguments

`x`	numeric vector, observations x
`null`	cumulative distribution function
`alternative`	character scalar, alternative hypothesis, either `'two.sided'` (default), `'less'`, or `'greater'`
`...`	additional arguments of `null`

Details

Function `Kolmogorov_dist()` is different from ks.test in the following aspects

- Ties in observations are supported. The step function of empirical distribution is inspired by ecdf. This is superior than `(0:(n - 1))/n` in ks.test.
- Discrete distribution (with discrete observation) is supported.
- Discrete distribution (with continuous observation) is not supported yet. This will be an easy modification in future.
- Only the one-sample Kolmogorov distance, not the one-sample Kolmogorov test, is returned, to speed up the calculation.

Value

Function `Kolmogorov_dist()` returns a numeric scalar.

Examples

```
# from ?stats::ks.test
x1 = rnorm(50)
ks.test(x1+2, y = pgamma, shape = 3, rate = 2)
Kolmogorov_dist(x1+2, null = pgamma, shape = 3, rate = 2) # exactly the same

# discrete distribution
x2 <- rnbinom(n = 1e2L, size = 500, prob = .4)
suppressWarnings(ks.test(x2, y = pnbinom, size = 500, prob = .4)) # warning on ties
Kolmogorov_dist(x2, null = pnbinom, size = 500, prob = .4) # wont be the same
```

`mlogis` *Multinomial Probabilities & Logits*

Description

Performs transformation between vectors of multinomial probabilities and multinomial logits.

This transformation is a generalization of plogis which converts scalar logit into probability and qlogis which converts probability into scalar logit.

Usage

```
qmlogis_first(p)

qmlogis_last(p)

pmlogis_first(q)

pmlogis_last(q)
```

Arguments

`p`	numeric vector, multinomial probabilities, adding up to 1
`q`	numeric vector, multinomial logits

Details

Functions pmlogis_first and pmlogis_last take a length $k-1$ numeric vector of multinomial logits q and convert them into length k multinomial probabilities p, regarding the first or last category as reference, respectively.

Functions qmlogis_first and qmlogis_last take a length k numeric vector of multinomial probabilities p and convert them into length $k-1$ multinomial logits q, regarding the first or last category as reference, respectively.

Value

Functions pmlogis_first and pmlogis_last return a vector of multinomial probabilities p.

Functions qmlogis_first and qmlogis_last return a vector of multinomial logits q.

See Also

plogis qlogis

Examples

```
(a = qmlogis_last(c(2,5,3)))
(b = qmlogis_first(c(2,5,3)))
pmlogis_last(a)
pmlogis_first(b)

q0 = .8300964
(p1 = pmlogis_last(q0))
(q1 = qmlogis_last(p1))

# various exceptions
pmlogis_first(qmlogis_first(c(1, 0)))
pmlogis_first(qmlogis_first(c(0, 1)))
pmlogis_first(qmlogis_first(c(0, 0, 1)))
pmlogis_first(qmlogis_first(c(0, 1, 0, 0)))
pmlogis_first(qmlogis_first(c(1, 0, 0, 0)))
pmlogis_last(qmlogis_last(c(1, 0)))
pmlogis_last(qmlogis_last(c(0, 1)))
pmlogis_last(qmlogis_last(c(0, 0, 1)))
pmlogis_last(qmlogis_last(c(0, 1, 0, 0)))
pmlogis_last(qmlogis_last(c(1, 0, 0, 0)))
```

---

moment2fmx *Creates fmx Object with Given Component-Wise Moments*

Description

Creates fmx Object with Given Component-Wise Moments

Usage

```
moment2fmx(distname, w, ...)
```

Arguments

distname	character scalar
w	numeric vector
...	numeric scalars, some or all of mean, sd, skewness and kurtosis (length will be recycled), see moment2param

Value

Function moment2fmx() returns a fmx object.

Examples

```
m = c(-1.5, 1.5)
s = c(.9, 1.1)
sk = c(.2, -.3)
kt = c(.5, .75)
w = c(2, 3)
(d1 = moment2fmx(distname='GH', w=w, mean=m, sd=s, skewness=sk, kurtosis=kt))
moment_fmx(d1)
(d2 = moment2fmx(distname='st', w=w, mean=m, sd=s, skewness=sk, kurtosis=kt))
moment_fmx(d2)
library(ggplot2)
ggplot() +
 geom_function(aes(color = 'GH'), fun = dfmx, args = list(dist=d1), n = 1001) +
 geom_function(aes(color = 'st'), fun = dfmx, args = list(dist=d1), n = 1001) +
 xlim(-5, 6)
# two curves looks really close, but actually not identical
x = rfmx(n = 1e3L, dist = d1)
range(dfmx(x, dist = d1) - dfmx(x, dist = d2))
```

`moment_fmx` *Moment of Each Component in an fmx Object*

Description

To find moments of each component in an fmx object.

Usage

```
moment_fmx(object)
```

Arguments

`object`	an fmx object

Details

Function `moment_fmx()` calculates the moments and distribution characteristics of each mixture component of an S4 fmx object.

Value

Function `moment_fmx()` returns a moment object.

Examples

```
(d2 = fmx('GH', A = c(1,6), B = 2, g = c(0,.3), h = c(.2,0), w = c(1,2)))
moment_fmx(d2)
```

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