

Package ‘densityratio’

July 22, 2025

Type Package

Title Distribution Comparison Through Density Ratio Estimation

Version 0.2.2

Description Fast, flexible and user-friendly tools for distribution comparison through direct density ratio estimation. The estimated density ratio can be used for covariate shift adjustment, outlier-detection, change-point detection, classification and evaluation of synthetic data quality. The package implements multiple non-parametric estimation techniques (unconstrained least-squares importance fitting, `ulsif()`, Kullback-Leibler importance estimation procedure, `klipe()`, spectral density ratio estimation, `spectral()`, kernel mean matching, `kmm()`, and least-squares hetero-distributional subspace search, `lhss()`), with automatic tuning of hyperparameters. Helper functions are available for two-sample testing and visualizing the density ratios. For an overview on density ratio estimation, see Sugiyama et al. (2012) <[doi:10.1017/CBO9781139035613](https://doi.org/10.1017/CBO9781139035613)> for a general overview, and the help files for references on the specific estimation techniques.

License GPL (>= 3)

Encoding UTF-8

LazyData true

Imports osqp, Rcpp, pbapply, ggplot2, ggh4x

LinkingTo Rcpp, RcppArmadillo, RcppProgress

Suggests knitr, rmarkdown, testthat (>= 3.0.0)

Config/testthat/edition 3

Config/testthat/parallel true

Depends R (>= 2.10)

RoxygenNote 7.3.2

VignetteBuilder knitr

URL <https://thomvolker.github.io/densityratio/>,
<https://github.com/thomvolker/densityratio>

BugReports <https://github.com/thomvolker/densityratio/issues>

NeedsCompilation yes

Author Thom Volker [aut, cre] (ORCID: <<https://orcid.org/0000-0002-2408-7820>>),
 Carlos Gonzalez Poses [ctb],
 Erik-Jan van Kesteren [ctb]

Maintainer Thom Volker <thombenjaminvolker@gmail.com>

Repository CRAN

Date/Publication 2025-07-18 16:40:02 UTC

Contents

colon	3
create_bivariate_plot	3
create_univariate_plot	4
denominator_data	4
denominator_small	5
distance	5
dr.histogram	6
insurance	8
kernel_gaussian	9
kidiq	9
kliep	10
kmm	11
lhss	13
naive	15
numerator_data	17
numerator_small	17
permute	18
plot_bivariate	19
plot_univariate	20
predict.kliep	22
predict.kmm	23
predict.lhss	24
predict.naivedensityratio	25
predict.spectral	26
predict.ulsif	27
print.kliep	28
print.kmm	29
print.lhss	30
print.naivedensityratio	31
print.spectral	32
print.summary.kliep	33
print.summary.kmm	34
print.summary.lhss	35
print.summary.naivedensityratio	36
print.summary.spectral	37
print.summary.ulsif	38

print.ulsif	39
spectral	40
summary.kliep	42
summary.kmm	43
summary.lhss	44
summary.naivedensityratio	46
summary.spectral	47
summary.ulsif	48
ulsif	49

Index	52
--------------	-----------

colon	<i>colon</i>
-------	--------------

Description

Colon cancer data set from princeton, containing 2000 gene expressions from 22 colon tumor tissues and 40 non-tumor tissues. The data is collected by Alon et al. (1999) and can be obtained from [here](#).

Format

A data.frame with 62 rows and 2001 columns (class variable and 2000 gene expressions).

create_bivariate_plot	<i>Bivariate plot</i>
-----------------------	-----------------------

Description

Bivariate plot

Usage

```
create_bivariate_plot(data, ext, vars, logscale, show.sample)
```

Arguments

data	Data frame with the individual values and density ratio estimates
ext	Data frame with the density ratio estimates and sample indicator
vars	Character vector of variable names to be plotted.
logscale	Logical indicating whether the density ratio should be plotted in log scale. Defaults to TRUE.
show.sample	Logical indicating whether to give different shapes to observations, depending on the sample they come from (numerator or denominator). Defaults to FALSE.

Value

Bivariate plot

`create_univariate_plot`

Univariate plot

Description

Scatterplot of individual values and density ratio estimates. Used internally in `create_univariate_plot()`

Usage

```
create_univariate_plot(data, ext, var, y_lab, sample.facet = TRUE)
```

Arguments

<code>data</code>	Data frame with the individual values and density ratio estimates
<code>ext</code>	Data frame with the density ratio estimates and sample indicator
<code>var</code>	Name of the variable to be plotted on the x-axis
<code>y_lab</code>	Name of the y-axis label, typically ("Density Ratio" or "Log Density Ratio")
<code>sample.facet</code>	Logical indicating whether to facet the plot by sample. Default is TRUE.

Value

A scatterplot of variable values and density ratio estimates.

<code>denominator_data</code>	<i>denominator_data</i>
-------------------------------	-------------------------

Description

Simulated data set (see `data-row/generate-data-densityratio.R`) with five variables that are used in the examples.

Format

A data frame with 1000 rows and 5 columns:

- x1** Categorical variable with three categories, 'A', 'B' and 'C'
- x2** Categorical variable with two categories, 'G1' and 'G2'
- x3** Continuous variable (normally distributed given x1 and x2)
- x4** Continuous variable (normally distributed)
- x5** Continuous variable (normally distributed)

denominator_small	<i>denominator_small</i>
-------------------	--------------------------

Description

Subset of the [denominator_data](#) with three variables and 50 observations

Format

- A data frame with 100 rows and 3 columns:
- x1** Continuous variable (normally distributed given x1 and x2)
 - x2** Continuous variable (normally distributed)
 - x3** Continuous variable (normally distributed)

distance	<i>Create a Gram matrix with squared Euclidean distances between observations in the input matrix X and the input matrix Y</i>
----------	--

Description

Create a Gram matrix with squared Euclidean distances between observations in the input matrix X and the input matrix Y

Arguments

- X A numeric input matrix
- Y A numeric input matrix with the same variables as X
- intercept Logical indicating whether an intercept should be added to the estimation procedure. In this case, the first column is an all-zero column (which will be transformed into an all-ones column in the kernel).

`dr.histogram`*A histogram of density ratio estimates*

Description

Creates a histogram of the density ratio estimates. Useful to understand the distribution of estimated density ratios in each sample, or compare it among samples. It is the default plotting method for density ratio objects.

Usage

```
dr.histogram(  
  x,  
  samples = "both",  
  logscale = TRUE,  
  binwidth = NULL,  
  bins = NULL,  
  tol = 0.01,  
  ...  
)  
  
## S3 method for class 'ulsif'  
plot(  
  x,  
  samples = "both",  
  logscale = TRUE,  
  binwidth = NULL,  
  bins = NULL,  
  tol = 0.01,  
  ...  
)  
  
## S3 method for class 'klienp'  
plot(  
  x,  
  samples = "both",  
  logscale = TRUE,  
  binwidth = NULL,  
  bins = NULL,  
  tol = 0.01,  
  ...  
)  
  
## S3 method for class 'kmm'  
plot(  
  x,  
  samples = "both",
```

```

    logscale = TRUE,
    binwidth = NULL,
    bins = NULL,
    tol = 0.01,
    ...
)

## S3 method for class 'spectral'
plot(
  x,
  samples = "both",
  logscale = TRUE,
  binwidth = NULL,
  bins = NULL,
  tol = 0.01,
  ...
)

## S3 method for class 'lhss'
plot(
  x,
  samples = "both",
  logscale = TRUE,
  binwidth = NULL,
  bins = NULL,
  tol = 0.01,
  ...
)

## S3 method for class 'naivedensityratio'
plot(
  x,
  samples = "both",
  logscale = TRUE,
  binwidth = NULL,
  bins = NULL,
  tol = 0.01,
  ...
)

```

Arguments

x	Density ratio object created with e.g., <code>klipe()</code> , <code>ulsif()</code> , or <code>naive()</code>
samples	Character string indicating whether to plot the 'numerator', 'denominator', or 'both' samples. Default is 'both'.
logscale	Logical indicating whether to plot the density ratio estimates on a log scale. Default is TRUE.
binwidth	Numeric indicating the width of the bins, passed on to <code>ggplot2</code> .

<code>bins</code>	Numeric indicating the number of bins. Overriden by <code>binwidth</code> , and passed on to <code>ggplot2</code> .
<code>tol</code>	Numeric indicating the tolerance: values below this value will be set to the tolerance value, for legibility of the plots
<code>...</code>	Additional arguments passed on to <code>predict()</code> .

Value

A histogram of density ratio estimates.
 A histogram of density ratio estimates.
 A histogram of density ratio estimates.
 A histogram of density ratio estimates.
 A histogram of density ratio estimates.
 A histogram of density ratio estimates.
 A histogram of density ratio estimates.

See Also

[ulsif](#) for example usage
[kliep](#) for example usage
[kmm](#) for example usage
[spectral](#) for example usage
[lhss](#) for example usage
[naive](#) for example usage

insurance

insurance

Description

Insurance data that is openly available (e.g., on [Kaggle](#)).

Format

A `data.frame` with 1338 rows and 7 columns:

age Age of the insured (continuous)
sex Sex of the insured (binary)
bmi Body mass index of the insured (continuous)
children Number of children/dependents covered by the insurance (integer)
smoker Whether the insured is a smoker (binary)
region The region in which the insured lives (categorical)
charges The medical costs billed by the insurance (continuous)

kernel_gaussian	Create gaussian kernel gram matrix from distance matrix
-----------------	---

Description

Create gaussian kernel gram matrix from distance matrix

Arguments

dist	A numeric distance matrix
sigma	A scalar with the length-scale parameter

kidiq	<i>kidiq</i>
-------	--------------

Description

The kidiq data stems from the National Longitudinal Survey of Youth and is used in Gelman and Hill (2007). The data set contains 434 observations measured on five variables, and is obtained from <https://github.com/jknowles/BDAexampleR>.

Format

A data.frame with 434 rows and 5 columns

kid_score Child's IQ score (continuous)

mom_hs Whether the mother obtained a high school degree (binary)

mom_iq Mother's IQ score (continuous)

mom_work Whether the mother worked in the first three years of the child's life (1: not in the first three years; 2: in the second or third year; 3: parttime in the first year; 4: fulltime in the first year)

mom_age Mother's age (continuous)

klien

*Kullback-Leibler importance estimation procedure***Description**

Kullback-Leibler importance estimation procedure

Usage

```
klien(
  df_numerator,
  df_denominator,
  scale = "numerator",
  nsigma = 10,
  sigma_quantile = NULL,
  sigma = NULL,
  ncenters = 200,
  centers = NULL,
  cv = TRUE,
  nfold = 5,
  epsilon = NULL,
  maxit = 5000,
  progressbar = TRUE
)
```

Arguments

<code>df_numerator</code>	data.frame with exclusively numeric variables with the numerator samples
<code>df_denominator</code>	data.frame with exclusively numeric variables with the denominator samples (must have the same variables as <code>df_denominator</code>)
<code>scale</code>	"numerator", "denominator", or NULL, indicating whether to standardize each numeric variable according to the numerator means and standard deviations, the denominator means and standard deviations, or apply no standardization at all.
<code>nsigma</code>	Integer indicating the number of sigma values (bandwidth parameter of the Gaussian kernel gram matrix) to use in cross-validation.
<code>sigma_quantile</code>	NULL or numeric vector with probabilities to calculate the quantiles of the distance matrix to obtain sigma values. If NULL, <code>nsigma</code> values between 0.25 and 0.75 are used.
<code>sigma</code>	NULL or a scalar value to determine the bandwidth of the Gaussian kernel gram matrix. If NULL, <code>nsigma</code> values between 0.25 and 0.75 are used.
<code>ncenters</code>	Maximum number of Gaussian centers in the kernel gram matrix. Defaults to all numerator samples.
<code>centers</code>	Option to specify the Gaussian samples manually.
<code>cv</code>	Logical indicating whether or not to do cross-validation

<code>nfold</code>	Number of cross-validation folds used in order to calculate the optimal sigma value (default is 5-fold cv).
<code>epsilon</code>	Numeric scalar or vector with the learning rate for the gradient-ascent procedure. If a vector, all values are used as the learning rate. By default, $10^{\{1:-5\}}$ is used.
<code>maxit</code>	Maximum number of iterations for the optimization scheme.
<code>progressbar</code>	Logical indicating whether or not to display a progressbar.

Value

`klied`-object, containing all information to calculate the density ratio using optimal sigma and optimal weights.

References

Sugiyama, M., Suzuki, T., Nakajima, S., Kashima, H., Von Büna, P., & Kawanabe, M. (2008). Direct importance estimation for covariate shift adaptation. *Annals of the Institute of Statistical Mathematics* 60, 699-746. Doi: <https://doi.org/10.1007/s10463-008-0197-x>.

Examples

```
set.seed(123)
# Fit model
dr <- klied(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
klied(numerator_small, denominator_small,
      nsigma = 1, ncenters = 100, nfold = 10,
      epsilon = 10^{\{2:-5\}}, maxit = 500)
```

Description

Kernel mean matching approach to density ratio estimation

Usage

```
kmm(
  df_numerator,
  df_denominator,
  scale = "numerator",
  constrained = FALSE,
  nsigma = 10,
  sigma_quantile = NULL,
  sigma = NULL,
  ncenters = 200,
  centers = NULL,
  cv = TRUE,
  nfold = 5,
  parallel = FALSE,
  nthreads = NULL,
  progressbar = TRUE,
  osqp_settings = NULL,
  cluster = NULL
)
```

Arguments

<code>df_numerator</code>	data.frame with exclusively numeric variables with the numerator samples
<code>df_denominator</code>	data.frame with exclusively numeric variables with the denominator samples (must have the same variables as <code>df_numerator</code>)
<code>scale</code>	"numerator", "denominator", or NULL, indicating whether to standardize each numeric variable according to the numerator means and standard deviations, the denominator means and standard deviations, or apply no standardization at all.
<code>constrained</code>	logical equals FALSE to use unconstrained optimization, TRUE to use constrained optimization. Defaults to FALSE.
<code>nsigma</code>	Integer indicating the number of sigma values (bandwidth parameter of the Gaussian kernel gram matrix) to use in cross-validation.
<code>sigma_quantile</code>	NULL or numeric vector with probabilities to calculate the quantiles of the distance matrix to obtain sigma values. If NULL, nsigma values between 0.25 and 0.75 are used.
<code>sigma</code>	NULL or a scalar value to determine the bandwidth of the Gaussian kernel gram matrix. If NULL, nsigma values between 0.25 and 0.75 are used.
<code>ncenters</code>	Maximum number of Gaussian centers in the kernel gram matrix. Defaults to all numerator samples.
<code>centers</code>	Option to specify the Gaussian samples manually.
<code>cv</code>	Logical indicating whether or not to do cross-validation
<code>nfold</code>	Number of cross-validation folds used in order to calculate the optimal sigma value (default is 5-fold cv).
<code>parallel</code>	logical indicating whether to use parallel processing in the cross-validation scheme.

nthreads	NULL or integer indicating the number of threads to use for parallel processing. If parallel processing is enabled, it defaults to the number of available threads minus one.
progressbar	Logical indicating whether or not to display a progressbar.
osqp_settings	Optional: settings to pass to the osqp solver for constrained optimization.
cluster	Optional: a cluster object to use for parallel processing, see <code>parallel::makeCluster</code> .

Value

kmm-object, containing all information to calculate the density ratio using optimal sigma and optimal weights.

References

Huang, J., Smola, A. J., Gretton, A., Borgwardt, K. M., & Schölkopf, B. (2006). Correcting sample selection bias by unlabeled data. In *Advances in Neural Information Processing Systems*, edited by B. Schölkopf, J. Platt and T. Hoffman. Available from <https://proceedings.neurips.cc/paper/2006/hash/a2186aa7c086b46ad4e8bf81e2a3a19b-Abstract.html>.

Examples

```
set.seed(123)
# Fit model
dr <- kmm(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
kmm(numerator_small, denominator_small,
     nsigma = 5, ncenters = 100, nfold = 10,
     constrained = TRUE)
```

Description

Least-squares heterodistributional subspace search

Usage

```
lhss(
  df_numerator,
  df_denominator,
  m = NULL,
  intercept = TRUE,
  scale = "numerator",
  nsigma = 10,
  sigma_quantile = NULL,
  sigma = NULL,
  nlambda = 10,
  lambda = NULL,
  ncenters = 200,
  centers = NULL,
  maxit = 200,
  progressbar = TRUE
)
```

Arguments

<code>df_numerator</code>	data.frame with exclusively numeric variables with the numerator samples
<code>df_denominator</code>	data.frame with exclusively numeric variables with the denominator samples (must have the same variables as <code>df_denominator</code>)
<code>m</code>	Scalar indicating the dimensionality of the reduced subspace
<code>intercept</code>	logical Indicating whether to include an intercept term in the model. Defaults to TRUE.
<code>scale</code>	"numerator", "denominator", or NULL, indicating whether to standardize each numeric variable according to the numerator means and standard deviations, the denominator means and standard deviations, or apply no standardization at all.
<code>nsigma</code>	Integer indicating the number of sigma values (bandwidth parameter of the Gaussian kernel gram matrix) to use in cross-validation.
<code>sigma_quantile</code>	NULL or numeric vector with probabilities to calculate the quantiles of the distance matrix to obtain sigma values. If NULL, nsigma values between 0.05 and 0.95 are used.
<code>sigma</code>	NULL or a scalar value to determine the bandwidth of the Gaussian kernel gram matrix. If NULL, nsigma values between 0.05 and 0.95 are used.
<code>nlambda</code>	Integer indicating the number of lambda values (regularization parameter), by default, lambda is set to $10^{\text{seq}(3, -3, \text{length.out} = \text{nlambda})}$.
<code>lambda</code>	NULL or numeric vector indicating the lambda values to use in cross-validation
<code>ncenters</code>	Maximum number of Gaussian centers in the kernel gram matrix. Defaults to all numerator samples.
<code>centers</code>	Numeric matrix with the same variables as <code>nu</code> and <code>de</code> that are used as Gaussian centers in the kernel Gram matrix. By default, the matrix <code>nu</code> is used as the matrix with Gaussian centers.
<code>maxit</code>	Maximum number of iterations in the updating scheme.
<code>progressbar</code>	Logical indicating whether or not to display a progressbar.

Value

lhss-object, containing all information to calculate the density ratio using optimal sigma, optimal lambda and optimal weights.

References

Sugiyama, M., Yamada, M., Von Büna, P., Suzuki, T., Kanamori, T. & Kawanabe, M. (2011). Direct density-ratio estimation with dimensionality reduction via least-squares hetero-distributional subspace search. *Neural Networks*, 24, 183-198. doi:[10.1016/j.neunet.2010.10.005](https://doi.org/10.1016/j.neunet.2010.10.005).

Examples

```
set.seed(123)
# Fit model
dr <- naive(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
naive(numerator_small, denominator_small, m=2, kernel="epanechnikov")
```

naive

Naive density ratio estimation

Description

The naive approach creates separate kernel density estimates for the numerator and the denominator samples, and then evaluates their ratio for the denominator samples. For multivariate data, the density ratio is computed after a orthogonal linear transformation, such that the new variables can be treated as independent. To reduce the dimensionality of the PCA solution, one can set the number of components by setting the `m` parameter to an integer value smaller than the number of variables.

Usage

```
naive(
  df_numerator,
  df_denominator,
  m = NULL,
  bw = "SJ",
```

```

    kernel = "gaussian",
    n = 2L^11,
    ...
)

```

Arguments

<code>df_numerator</code>	data.frame with exclusively numeric variables with the numerator samples
<code>df_denominator</code>	data.frame with exclusively numeric variables with the denominator samples (must have the same variables as <code>df_numerator</code>)
<code>m</code>	integer Optional parameter to reduce the dimensionality of the data in multi-variate density ratio estimation problems. If missing, the number of variables in the data is used. If set to an integer value smaller than the number of variables, the first <code>m</code> principal components are used to estimate the density ratio. If set to <code>NULL</code> , the square root of the number of variables is used (for consistency with other methods).
<code>bw</code>	the smoothing bandwidth to be used. See stats::density for more information.
<code>kernel</code>	the kernel to be used. See stats::density for more information.
<code>n</code>	integer the number of equally spaced points at which the density is to be estimated. When <code>n > 512</code> , it is rounded up to a power of 2 during the calculations (as fast Fourier transform is used) and the final result is interpolated by stats::approx . So it makes sense to specify <code>n</code> as a power of two.
<code>...</code>	further arguments passed to stats::density

Value

naivedensityratio object

See Also

[stats::density\(\)](#)

Examples

```

set.seed(123)
# Fit model
dr <- naive(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))

```

```
# Fit model with custom parameters
naive(numerator_small, denominator_small, m=2, kernel="epanechnikov")
```

numerator_data	<i>numerator_data</i>
----------------	-----------------------

Description

Simulated data set (see `data-raw/generate-data-densityratio.R`) with five variables that are used in the examples.

Format

A data frame with 1000 rows and 5 columns:

- x1** Categorical variable with three categories, 'A', 'B' and 'C'
- x2** Categorical variable with two categories, 'G1' and 'G2'
- x3** Continuous variable (normally distributed given x1 and x2)
- x4** Continuous variable (normally distributed given x3)
- x5** Continuous variable (mixture of two normally distributed variables)

numerator_small	<i>numerator_small</i>
-----------------	------------------------

Description

Subset of the [numerator_data](#) with three variables and 50 observations

Format

A data frame with 50 rows and 3 columns:

- x1** Continuous variable (normally distributed given x1 and x2)
- x2** Continuous variable (normally distributed given x3)
- x3** Continuous variable (mixture of two normally distributed variables)

permute	<i>Single permutation</i>
---------	---------------------------

Description

Single permutation
 Single permutation statistic of `ulsif` object
 Single permutation statistic of `klied` object
 Single permutation statistic of `kmm` object
 Single permutation statistic of `lhss` object
 Single permutation statistic of `spectral` object
 Single permutation statistic of `naivedensityratio` object

Usage

```

permute(object, ...)

## S3 method for class 'ulsif'
permute(object, stacked, nnu, nde, ...)

## S3 method for class 'klied'
permute(object, stacked, nnu, nde, min_pred = sqrt(.Machine$double.eps), ...)

## S3 method for class 'kmm'
permute(object, stacked, nnu, nde, ...)

## S3 method for class 'lhss'
permute(object, stacked, nnu, nde, ...)

## S3 method for class 'spectral'
permute(object, stacked, nnu, nde, ...)

## S3 method for class 'naivedensityratio'
permute(object, stacked, nnu, nde, min_pred, max_pred, ...)

```

Arguments

<code>object</code>	<code>naivedensityratio</code> object
<code>...</code>	Additional arguments to pass through to specific permute functions.
<code>stacked</code>	matrix with stacked numerator and denominator samples
<code>nnu</code>	Scalar with numerator sample size
<code>nde</code>	Scalar with denominator sample size
<code>min_pred</code>	Minimum value of the predicted density ratio
<code>max_pred</code>	Maximum value of the predicted density ratio

Value

permutation statistic for a single permutation of the data
 permutation statistic for a single permutation of the data
 permutation statistic for a single permutation of the data
 permutation statistic for a single permutation of the data
 permutation statistic for a single permutation of the data
 permutation statistic for a single permutation of the data
 permutation statistic for a single permutation of the data

plot_bivariate	<i>Densityratio in two-dimensional plot</i>
----------------	---

Description

Plots a scatterplot of two variables, with densityratio mapped to the colour scale.

Usage

```
plot_bivariate(
  x,
  vars = NULL,
  samples = "both",
  grid = FALSE,
  logscale = TRUE,
  show.sample = FALSE,
  tol = 0.01,
  ...
)
```

Arguments

x	Density ratio object created with e.g., <code>klipe()</code> , <code>ulsif()</code> , or <code>naive()</code>
vars	Character vector of variable names for which all pairwise bivariate plots are created
samples	Character string indicating whether to plot the 'numerator', 'denominator', or 'both' samples. Default is 'both'.
grid	Logical indicating whether output should be a list of individual plots ("individual"), or one faceted plot with all variables ("assembled"). Defaults to "individual".
logscale	Logical indicating whether to plot the density ratio estimates on a log scale. Default is TRUE.
show.sample	Logical indicating whether to give different shapes to observations, depending on the sample they come from (numerator or denominator). Defaults to FALSE.

tol	Numeric indicating the tolerance: values below this value will be set to the tolerance value, for legibility of the plots
...	Additional arguments passed to the predict() function.

Value

Bivariate scatter plots of all combinations of variables in vars.

Examples

```
set.seed(123)
# Fit model
dr <- ulsif(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
ulsif(numerator_small, denominator_small, sigma = 2, lambda = 2)
```

plot_univariate	<i>Scatter plot of density ratios and individual variables</i>
-----------------	--

Description

A scatter plot showing the relationship between estimated density ratios and individual variables.

Usage

```
plot_univariate(
  x,
  vars = NULL,
  samples = "both",
  logscale = TRUE,
  grid = FALSE,
  sample.facet = FALSE,
  nrow.panel = NULL,
  tol = 0.01,
  ...
)
```

Arguments

<code>x</code>	Density ratio object created with e.g., <code>klietp()</code> , <code>ulsif()</code> , or <code>naive()</code>
<code>vars</code>	Character vector of variable names to be plotted.
<code>samples</code>	Character string indicating whether to plot the 'numerator', 'denominator', or 'both' samples. Default is 'both'.
<code>logscale</code>	Logical indicating whether to plot the density ratio estimates on a log scale. Default is TRUE.
<code>grid</code>	Logical indicating whether output should be a list of individual plots ("individual"), or one faceted plot with all variables ("assembled"). Defaults to "individual".
<code>sample.facet</code>	Logical indicating whether to facet the plot by sample, i.e, showing plots separate for each sample, and side to side. Defaults to FALSE.
<code>nrow.panel</code>	Integer indicating the number of rows in the assembled plot. If NULL, the number of rows is automatically calculated.
<code>tol</code>	Numeric indicating the tolerance: values below this value will be set to the tolerance value, for legibility of the plots
<code>...</code>	Additional arguments passed to the <code>predict()</code> function.

Value

Scatter plot of density ratios and individual variables.

Examples

```

set.seed(123)
# Fit model
dr <- ulsif(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
ulsif(numerator_small, denominator_small, sigma = 2, lambda = 2)

```

predict.kliep	<i>Obtain predicted density ratio values from a kliep object</i>
---------------	--

Description

Obtain predicted density ratio values from a kliep object

Usage

```
## S3 method for class 'kliep'
predict(object, newdata = NULL, sigma = c("sigmaopt", "all"), ...)
```

Arguments

object	A kliep object
newdata	Optional matrix new data set to compute the density
sigma	A scalar with the Gaussian kernel width
...	Additional arguments to be passed to the function

Value

An array with predicted density ratio values from possibly new data, but otherwise the numerator samples.

See Also

[predict, kliep](#)

Examples

```
set.seed(123)
# Fit model
dr <- kliep(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
kliep(numerator_small, denominator_small,
      nsigma = 1, ncenters = 100, nfold = 10,
      epsilon = 10^{2:-5}, maxit = 500)
```

predict.kmm	<i>Obtain predicted density ratio values from a kmm object</i>
-------------	--

Description

Obtain predicted density ratio values from a kmm object

Usage

```
## S3 method for class 'kmm'  
predict(object, newdata = NULL, sigma = c("sigmaopt", "all"), ...)
```

Arguments

object	A kmm object
newdata	Optional matrix new data set to compute the density
sigma	A scalar with the Gaussian kernel width
...	Additional arguments to be passed to the function

Value

An array with predicted density ratio values from possibly new data, but otherwise the numerator samples.

See Also

[predict, kmm](#)

Examples

```
set.seed(123)  
# Fit model  
dr <- kmm(numerator_small, denominator_small)  
# Inspect model object  
dr  
# Obtain summary of model object  
summary(dr)  
# Plot model object  
plot(dr)  
# Plot density ratio for each variable individually  
plot_univariate(dr)  
# Plot density ratio for each pair of variables  
plot_bivariate(dr)  
# Predict density ratio and inspect first 6 predictions  
head(predict(dr))  
# Fit model with custom parameters  
kmm(numerator_small, denominator_small,  
     nsigma = 5, ncenters = 100, nfold = 10,
```

```
constrained = TRUE)
```

predict.lhss

Obtain predicted density ratio values from a lhss object

Description

Obtain predicted density ratio values from a lhss object

Usage

```
## S3 method for class 'lhss'
predict(
  object,
  newdata = NULL,
  sigma = c("sigmaopt", "all"),
  lambda = c("lambdaopt", "all"),
  ...
)
```

Arguments

object	A lhss object
newdata	Optional matrix new data set to compute the density
sigma	A scalar with the Gaussian kernel width
lambda	A scalar with the regularization parameter
...	Additional arguments to be passed to the function

Value

An array with predicted density ratio values from possibly new data, but otherwise the numerator samples.

See Also

[predict, lhss](#)

Examples

```
set.seed(123)
# Fit model (minimal example to limit computation time)
dr <- lhss(numerator_small, denominator_small,
          nsigma = 5, nlambda = 3, ncenters = 50, maxit = 100)
# Inspect model object
dr
# Obtain summary of model object
```

```
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
```

predict.naivedensityratio

Obtain predicted density ratio values from a naivedensityratio object

Description

Obtain predicted density ratio values from a naivedensityratio object

Usage

```
## S3 method for class 'naivedensityratio'
predict(object, newdata = NULL, log = FALSE, tol = 1e-06, ...)
```

Arguments

object	A naive object
newdata	Optional matrix new data set to compute the density
log	A logical indicating whether to return the log of the density ratio
tol	Minimal density value to avoid numerical issues
...	Additional arguments to be passed to the function

Value

An array with predicted density ratio values from possibly new data, but otherwise the numerator samples.

See Also

[predict, naive](#)

Examples

```

set.seed(123)
# Fit model
dr <- naive(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
naive(numerator_small, denominator_small, m=2, kernel="epanechnikov")

```

predict.spectral	<i>Obtain predicted density ratio values from a spectral object</i>
------------------	---

Description

Obtain predicted density ratio values from a spectral object

Usage

```

## S3 method for class 'spectral'
predict(
  object,
  newdata = NULL,
  sigma = c("sigmaopt", "all"),
  m = c("opt", "all"),
  ...
)

```

Arguments

object	A spectral object
newdata	Optional matrix new data set to compute the density
sigma	A scalar with the Gaussian kernel width
m	integer indicating the dimension of the eigenvector expansion
...	Additional arguments to be passed to the function

Value

An array with predicted density ratio values from possibly new data, but otherwise the numerator samples.

See Also

[predict](#), [spectral](#)

predict.ulsif	<i>Obtain predicted density ratio values from a ulsif object</i>
---------------	--

Description

Obtain predicted density ratio values from a ulsif object

Usage

```
## S3 method for class 'ulsif'
predict(
  object,
  newdata = NULL,
  sigma = c("sigmaopt", "all"),
  lambda = c("lambdaopt", "all"),
  ...
)
```

Arguments

object	A ulsif object
newdata	Optional matrix new data set to compute the density
sigma	A scalar with the Gaussian kernel width
lambda	A scalar with the regularization parameter
...	Additional arguments to be passed to the function

Value

An array with predicted density ratio values from possibly new data, but otherwise the numerator samples.

See Also

[predict](#), [ulsif](#)

Examples

```

set.seed(123)
# Fit model
dr <- ulsif(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
ulsif(numerator_small, denominator_small, sigma = 2, lambda = 2)

```

print.kliep

Print a kliep object

Description

Print a kliep object

Usage

```

## S3 method for class 'kliep'
print(x, digits = max(3L, getOption("digits") - 3L), ...)

```

Arguments

x	Object of class kliep.
digits	Number of digits to use when printing the output.
...	further arguments on how to format the number of digits.

Value

invisible The inputted kliep object.

See Also

[print, kliep](#)

Examples

```

set.seed(123)
# Fit model
dr <- kliep(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
kliep(numerator_small, denominator_small,
      nsigma = 1, ncenters = 100, nfold = 10,
      epsilon = 10^{2:-5}, maxit = 500)

```

print.kmm

Print a kmm object

Description

Print a kmm object

Usage

```

## S3 method for class 'kmm'
print(x, digits = max(3L, getOption("digits") - 3L), ...)

```

Arguments

x	Object of class kmm.
digits	Number of digits to use when printing the output.
...	further arguments on how to format the number of digits.

Value

invisible The inputted kmm object.

See Also

[print, kmm](#)

Examples

```

set.seed(123)
# Fit model
dr <- kmm(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
kmm(numerator_small, denominator_small,
    nsigma = 5, ncenters = 100, nfold = 10,
    constrained = TRUE)

```

print.lhss

Print a lhss object

Description

Print a lhss object

Usage

```

## S3 method for class 'lhss'
print(x, digits = max(3L, getOption("digits") - 3L), ...)

```

Arguments

x	Object of class lhss.
digits	Number of digits to use when printing the output.
...	further arguments on how to format the number of digits.

Value

invisible The inputted lhss object.

See Also

[print](#), [lhss](#)

Examples

```

set.seed(123)
# Fit model (minimal example to limit computation time)
dr <- lhss(numerator_small, denominator_small,
          nsigma = 5, nlambda = 3, ncenters = 50, maxit = 100)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))

```

```
print.naivedensityratio
```

Print a naive density ratio object

Description

Print a naive density ratio object

Usage

```
## S3 method for class 'naivedensityratio'
print(x, digits = max(3L, getOption("digits") - 3L), ...)
```

Arguments

x	Object of class <code>naivesubspacedensityratio</code> .
digits	Number of digits to use when printing the output.
...	further arguments on how to format the number of digits.

Value

invisible The inputted naive density ratio object.

See Also

[print](#), [naive](#)

Examples

```

set.seed(123)
# Fit model
dr <- naive(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
naive(numerator_small, denominator_small, m=2, kernel="epanechnikov")

```

<code>print.spectral</code>	<i>Print a spectral object</i>
-----------------------------	--------------------------------

Description

Print a spectral object

Usage

```

## S3 method for class 'spectral'
print(x, digits = max(3L, getOption("digits") - 3L), ...)

```

Arguments

<code>x</code>	Object of class <code>spectral</code> .
<code>digits</code>	Number of digits to use when printing the output.
<code>...</code>	further arguments on how to format the number of digits.

Value

`invisible` The inputted spectral object.

See Also

[print, spectral](#)

Examples

```

set.seed(123)
# Fit model
dr <- spectral(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
spectral(numerator_small, denominator_small, sigma = 2)

```

```
print.summary.kliep
```

Print a summary.kliep object

Description

Print a summary.kliep object

Usage

```
## S3 method for class 'summary.kliep'
print(x, digits = max(3L, getOption("digits") - 3L), ...)
```

Arguments

x	Object of class summary.kliep.
digits	Number of digits to use when printing the output.
...	further arguments on how to format the number of digits.

Value

invisible The inputted summary.kliep object.

See Also

[print](#), [summary.kliep](#), [kliep](#)

Examples

```

set.seed(123)
# Fit model
dr <- kliep(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
kliep(numerator_small, denominator_small,
      nsigma = 1, ncenters = 100, nfold = 10,
      epsilon = 10^{2:-5}, maxit = 500)

```

print.summary.kmm	<i>Print a summary.kmm object</i>
-------------------	-----------------------------------

Description

Print a summary.kmm object

Usage

```

## S3 method for class 'summary.kmm'
print(x, digits = max(3L, getOption("digits") - 3L), ...)

```

Arguments

x	Object of class summary.kmm.
digits	Number of digits to use when printing the output.
...	further arguments on how to format the number of digits.

Value

invisible The inputted summary.kmm object.

See Also

[print](#), [summary.kmm](#), [kmm](#)

Examples

```

set.seed(123)
# Fit model
dr <- kmm(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
kmm(numerator_small, denominator_small,
    nsigma = 5, ncenters = 100, nfold = 10,
    constrained = TRUE)

```

print.summary.lhss	<i>Print a summary.lhss object</i>
--------------------	------------------------------------

Description

Print a summary.lhss object

Usage

```

## S3 method for class 'summary.lhss'
print(x, digits = max(3L, getOption("digits") - 3L), ...)

```

Arguments

x	Object of class summary.lhss.
digits	Number of digits to use when printing the output.
...	further arguments on how to format the number of digits.

Value

invisible The inputted summary.lhss object.

See Also

[print](#), [summary.lhss](#), [lhss](#)

Examples

```

set.seed(123)
# Fit model (minimal example to limit computation time)
dr <- lhss(numerator_small, denominator_small,
          nsigma = 5, nlambda = 3, ncenters = 50, maxit = 100)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))

```

```
print.summary.naivedensityratio
```

Print a summary.naivedensityratio object

Description

Print a `summary.naivedensityratio` object

Usage

```
## S3 method for class 'summary.naivedensityratio'
print(x, digits = max(3L, getOption("digits") - 3L), ...)
```

Arguments

<code>x</code>	Object of class <code>summary.naivedensityratio</code> .
<code>digits</code>	Number of digits to use when printing the output.
<code>...</code>	further arguments on how to format the number of digits.

Value

invisible The inputted `summary.naivedensityratio` object.

See Also

[print](#), [summary.naivedensityratio](#), [naive](#)

Examples

```

set.seed(123)
# Fit model
dr <- naive(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
naive(numerator_small, denominator_small, m=2, kernel="epanechnikov")

```

```
print.summary.spectral
```

Print a summary.spectral object

Description

Print a summary.spectral object

Usage

```
## S3 method for class 'summary.spectral'
print(x, digits = max(3L, getOption("digits") - 3L), ...)
```

Arguments

x	Object of class summary.spectral.
digits	Number of digits to use when printing the output.
...	further arguments on how to format the number of digits.

Value

invisible The inputted summary.spectral object.

See Also

[print](#), [summary.spectral](#), [spectral](#)

Examples

```

set.seed(123)
# Fit model
dr <- spectral(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
spectral(numerator_small, denominator_small, sigma = 2)

```

```
print.summary.ulsif
```

Print a summary.ulsif object

Description

Print a `summary.ulsif` object

Usage

```
## S3 method for class 'summary.ulsif'
print(x, digits = max(3L, getOption("digits") - 3L), ...)
```

Arguments

<code>x</code>	Object of class <code>summary.ulsif</code> .
<code>digits</code>	Number of digits to use when printing the output.
<code>...</code>	further arguments on how to format the number of digits.

Value

`invisible` The inputted `summary.ulsif` object.

See Also

[print](#), [summary.ulsif](#), [ulsif](#)

Examples

```

set.seed(123)
# Fit model
dr <- ulsif(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
ulsif(numerator_small, denominator_small, sigma = 2, lambda = 2)

```

print.ulsif	<i>Print a ulsif object</i>
-------------	-----------------------------

Description

Print a ulsif object

Usage

```

## S3 method for class 'ulsif'
print(x, digits = max(3L, getOption("digits") - 3L), ...)

```

Arguments

x	Object of class ulsif.
digits	Number of digits to use when printing the output.
...	further arguments on how to format the number of digits.

Value

invisible The inputted ulsif object.

See Also

[print, ulsif](#)

Examples

```

set.seed(123)
# Fit model
dr <- ulsif(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
ulsif(numerator_small, denominator_small, sigma = 2, lambda = 2)

```

spectral

*Spectral series based density ratio estimation***Description**

Spectral series based density ratio estimation

Usage

```

spectral(
  df_numerator,
  df_denominator,
  m = NULL,
  scale = "numerator",
  nsigma = 10,
  sigma_quantile = NULL,
  sigma = NULL,
  ncenters = NULL,
  cv = TRUE,
  nfold = 10,
  parallel = FALSE,
  nthreads = NULL,
  progressbar = TRUE
)

```

Arguments

`df_numerator` data.frame with exclusively numeric variables with the numerator samples

<code>df_denominator</code>	data.frame with exclusively numeric variables with the denominator samples (must have the same variables as <code>df_denominator</code>)
<code>m</code>	Integer vector indicating the number of eigenvectors to use in the spectral series expansion. Defaults to 50 evenly spaced values between 1 and the number of denominator samples (or the largest number of samples that can be used as centers in the cross-validation scheme).
<code>scale</code>	"numerator", "denominator", or NULL, indicating whether to standardize each numeric variable according to the numerator means and standard deviations, the denominator means and standard deviations, or apply no standardization at all.
<code>nsigma</code>	Integer indicating the number of sigma values (bandwidth parameter of the Gaussian kernel gram matrix) to use in cross-validation.
<code>sigma_quantile</code>	NULL or numeric vector with probabilities to calculate the quantiles of the distance matrix to obtain sigma values. If NULL, <code>nsigma</code> values between 0.05 and 0.95 are used.
<code>sigma</code>	NULL or a scalar value to determine the bandwidth of the Gaussian kernel gram matrix. If NULL, <code>nsigma</code> values between 0.05 and 0.95 are used.
<code>ncenters</code>	integer If smaller than the number of denominator observations, an approximation to the eigenvector expansion based on only <code>ncenters</code> samples is performed, instead of the full expansion. This can be useful for large datasets. Defaults to NULL, such that all denominator samples are used.
<code>cv</code>	logical indicating whether to use cross-validation to determine the optimal sigma value and the optimal number of eigenvectors.
<code>nfold</code>	Integer indicating the number of folds to use in the cross-validation scheme. If <code>cv</code> is FALSE, this parameter is ignored.
<code>parallel</code>	logical indicating whether to use parallel processing in the cross-validation scheme.
<code>nthreads</code>	NULL or integer indicating the number of threads to use for parallel processing. If parallel processing is enabled, it defaults to the number of available threads minus one.
<code>progressbar</code>	Logical indicating whether or not to display a progressbar.

Value

spectral-object, containing all information to calculate the density ratio using optimal sigma and optimal spectral series expansion.

References

Izbicki, R., Lee, A. & Schafer, C. (2014). High-Dimensional Density Ratio Estimation with Extensions to Approximate Likelihood Computation. Proceedings of Machine Learning Research 33, 420-429. Available from <https://proceedings.mlr.press/v33/izbicki14.html>.

Examples

```
set.seed(123)
# Fit model
dr <- spectral(numerator_small, denominator_small)
```

```

# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
spectral(numerator_small, denominator_small, sigma = 2)

```

summary.kliep	<i>Extract summary from kliep object, including two-sample significance test for homogeneity of the numerator and denominator samples</i>
---------------	---

Description

Extract summary from kliep object, including two-sample significance test for homogeneity of the numerator and denominator samples

Usage

```

## S3 method for class 'kliep'
summary(
  object,
  test = FALSE,
  n_perm = 100,
  parallel = FALSE,
  cluster = NULL,
  min_pred = 1e-06,
  ...
)

```

Arguments

object	Object of class kliep
test	logical indicating whether to statistically test for homogeneity of the numerator and denominator samples.
n_perm	Scalar indicating number of permutation samples
parallel	logical indicating to run the permutation test in parallel
cluster	NULL or a cluster object created by makeCluster. If NULL and parallel = TRUE, it uses the number of available cores minus 1.
min_pred	Scalar indicating the minimum value for the predicted density ratio values (used in the divergence statistic) to avoid negative density ratio values.
...	further arguments passed to or from other methods.

Value

Summary of the fitted density ratio model

Examples

```
set.seed(123)
# Fit model
dr <- kliep(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
kliep(numerator_small, denominator_small,
      nsigma = 1, ncenters = 100, nfold = 10,
      epsilon = 10^{2:-5}, maxit = 500)
```

summary.kmm

Extract summary from kmm object, including two-sample significance test for homogeneity of the numerator and denominator samples

Description

Extract summary from kmm object, including two-sample significance test for homogeneity of the numerator and denominator samples

Usage

```
## S3 method for class 'kmm'
summary(
  object,
  test = FALSE,
  n_perm = 100,
  parallel = FALSE,
  cluster = NULL,
  min_pred = 1e-06,
  ...
)
```

Arguments

object	Object of class kmm
test	logical indicating whether to statistically test for homogeneity of the numerator and denominator samples.
n_perm	Scalar indicating number of permutation samples
parallel	logical indicating to run the permutation test in parallel
cluster	NULL or a cluster object created by makeCluster. If NULL and parallel = TRUE, it uses the number of available cores minus 1.
min_pred	Scalar indicating the minimum value for the predicted density ratio values (used in the divergence statistic) to avoid negative density ratio values.
...	further arguments passed to or from other methods.

Value

Summary of the fitted density ratio model

Examples

```
set.seed(123)
# Fit model
dr <- kmm(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
kmm(numerator_small, denominator_small,
    nsigma = 5, ncenters = 100, nfold = 10,
    constrained = TRUE)
```

summary.lhss

Extract summary from lhss object, including two-sample significance test for homogeneity of the numerator and denominator samples

Description

Extract summary from lhss object, including two-sample significance test for homogeneity of the numerator and denominator samples

Usage

```
## S3 method for class 'lhss'
summary(
  object,
  test = FALSE,
  n_perm = 100,
  parallel = FALSE,
  cluster = NULL,
  ...
)
```

Arguments

object	Object of class lhss
test	logical indicating whether to statistically test for homogeneity of the numerator and denominator samples.
n_perm	Scalar indicating number of permutation samples
parallel	logical indicating to run the permutation test in parallel
cluster	NULL or a cluster object created by makeCluster. If NULL and parallel = TRUE, it uses the number of available cores minus 1.
...	further arguments passed to or from other methods.

Value

Summary of the fitted density ratio model

Examples

```
set.seed(123)
# Fit model (minimal example to limit computation time)
dr <- lhss(numerator_small, denominator_small,
           nsigma = 5, nlambda = 3, ncenters = 50, maxit = 100)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
```

```
summary.naivedensityratio
```

Extract summary from naivedensityratio object, including two-sample significance test for homogeneity of the numerator and denominator samples

Description

Extract summary from naivedensityratio object, including two-sample significance test for homogeneity of the numerator and denominator samples

Usage

```
## S3 method for class 'naivedensityratio'
summary(
  object,
  test = FALSE,
  n_perm = 100,
  parallel = FALSE,
  cluster = NULL,
  ...
)
```

Arguments

object	Object of class naivedensityratio
test	logical indicating whether to statistically test for homogeneity of the numerator and denominator samples.
n_perm	Scalar indicating number of permutation samples
parallel	logical indicating to run the permutation test in parallel
cluster	NULL or a cluster object created by makeCluster. If NULL and parallel = TRUE, it uses the number of available cores minus 1.
...	further arguments passed to or from other methods.

Value

Summary of the fitted density ratio model

Examples

```
set.seed(123)
# Fit model
dr <- naive(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
```

```

summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
naive(numerator_small, denominator_small, m=2, kernel="epanechnikov")

```

summary.spectral	<i>Extract summary from spectral object, including two-sample significance test for homogeneity of the numerator and denominator samples</i>
------------------	--

Description

Extract summary from spectral object, including two-sample significance test for homogeneity of the numerator and denominator samples

Usage

```

## S3 method for class 'spectral'
summary(
  object,
  test = FALSE,
  n_perm = 100,
  parallel = FALSE,
  cluster = NULL,
  ...
)

```

Arguments

object	Object of class spectral
test	logical indicating whether to statistically test for homogeneity of the numerator and denominator samples.
n_perm	Scalar indicating number of permutation samples
parallel	logical indicating to run the permutation test in parallel
cluster	NULL or a cluster object created by makeCluster. If NULL and parallel = TRUE, it uses the number of available cores minus 1.
...	further arguments passed to or from other methods.

Value

Summary of the fitted density ratio model

Examples

```

set.seed(123)
# Fit model
dr <- spectral(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
spectral(numerator_small, denominator_small, sigma = 2)

```

summary.ulsif	<i>Extract summary from ulsif object, including two-sample significance test for homogeneity of the numerator and denominator samples</i>
---------------	---

Description

Extract summary from ulsif object, including two-sample significance test for homogeneity of the numerator and denominator samples

Usage

```

## S3 method for class 'ulsif'
summary(
  object,
  test = FALSE,
  n_perm = 100,
  parallel = FALSE,
  cluster = NULL,
  ...
)

```

Arguments

object	Object of class ulsif
test	logical indicating whether to statistically test for homogeneity of the numerator and denominator samples.
n_perm	Scalar indicating number of permutation samples
parallel	logical indicating to run the permutation test in parallel

cluster	NULL or a cluster object created by makeCluster. If NULL and parallel = TRUE, it uses the number of available cores minus 1.
...	further arguments passed to or from other methods.

Value

Summary of the fitted density ratio model

Examples

```
set.seed(123)
# Fit model
dr <- ulsif(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
ulsif(numerator_small, denominator_small, sigma = 2, lambda = 2)
```

ulsif

Unconstrained least-squares importance fitting

Description

Unconstrained least-squares importance fitting

Usage

```
ulsif(
  df_numerator,
  df_denominator,
  intercept = TRUE,
  scale = "numerator",
  nsigma = 10,
  sigma_quantile = NULL,
  sigma = NULL,
  nlambda = 20,
  lambda = NULL,
  ncenters = 200,
```

```

    centers = NULL,
    parallel = FALSE,
    nthreads = NULL,
    progressbar = TRUE
)

```

Arguments

<code>df_numerator</code>	data.frame with exclusively numeric variables with the numerator samples
<code>df_denominator</code>	data.frame with exclusively numeric variables with the denominator samples (must have the same variables as <code>df_numerator</code>)
<code>intercept</code>	logical Indicating whether to include an intercept term in the model. Defaults to TRUE.
<code>scale</code>	"numerator", "denominator", or NULL, indicating whether to standardize each numeric variable according to the numerator means and standard deviations, the denominator means and standard deviations, or apply no standardization at all.
<code>nsigma</code>	Integer indicating the number of sigma values (bandwidth parameter of the Gaussian kernel gram matrix) to use in cross-validation.
<code>sigma_quantile</code>	NULL or numeric vector with probabilities to calculate the quantiles of the distance matrix to obtain sigma values. If NULL, nsigma values between 0.05 and 0.95 are used.
<code>sigma</code>	NULL or a scalar value to determine the bandwidth of the Gaussian kernel gram matrix. If NULL, nsigma values between 0.05 and 0.95 are used.
<code>nlambda</code>	Integer indicating the number of lambda values (regularization parameter), by default, lambda is set to $10^{\text{seq}(3, -3, \text{length.out} = \text{nlambda})}$.
<code>lambda</code>	NULL or numeric vector indicating the lambda values to use in cross-validation
<code>ncenters</code>	Maximum number of Gaussian centers in the kernel gram matrix. Defaults to all numerator samples.
<code>centers</code>	NULL or numeric matrix with the same dimensions as the data, indicating the centers for the Gaussian kernel gram matrix.
<code>parallel</code>	logical indicating whether to use parallel processing in the cross-validation scheme.
<code>nthreads</code>	NULL or integer indicating the number of threads to use for parallel processing. If parallel processing is enabled, it defaults to the number of available threads minus one.
<code>progressbar</code>	Logical indicating whether or not to display a progressbar.

Value

ulsif-object, containing all information to calculate the density ratio using optimal sigma and optimal weights.

References

Kanamori, T., Hido, S., & Sugiyama, M. (2009). A least-squares approach to direct importance estimation. *Journal of Machine Learning Research*, 10, 1391-1445. Available from <https://jmlr.org/papers/v10/kanamori09a.html>

Examples

```
set.seed(123)
# Fit model
dr <- ulsif(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
ulsif(numerator_small, denominator_small, sigma = 2, lambda = 2)
```

Index

- * **colon**
 - colon, 3
- * **datasets**
 - colon, 3
 - denominator_data, 4
 - denominator_small, 5
 - insurance, 8
 - kidiq, 9
 - numerator_data, 17
 - numerator_small, 17
- * **data**
 - colon, 3
 - denominator_data, 4
 - denominator_small, 5
 - insurance, 8
 - kidiq, 9
 - numerator_data, 17
 - numerator_small, 17
- * **insurance**
 - insurance, 8
- * **kidiq**
 - kidiq, 9
- * **klied**
 - predict.klied, 22
- * **kmm**
 - predict.kmm, 23
- * **lhss**
 - predict.lhss, 24
- * **naive**
 - predict.naivedensityratio, 25
- * **predict**
 - predict.klied, 22
 - predict.kmm, 23
 - predict.lhss, 24
 - predict.naivedensityratio, 25
 - predict.spectral, 26
 - predict.ulsif, 27
- * **spectral**
 - predict.spectral, 26
- * **ulsif**
 - predict.ulsif, 27
- colon, 3
- create_bivariate_plot, 3
- create_univariate_plot, 4
- create_univariate_plot(), 4
- denominator_data, 4, 5
- denominator_small, 5
- distance, 5
- dr.histogram, 6
- insurance, 8
- kernel_gaussian, 9
- kidiq, 9
- klied, 8, 10, 22, 28, 33
- klied(), 7, 19, 21
- kmm, 8, 11, 23, 29, 34
- lhss, 8, 13, 24, 30, 35
- naive, 8, 15, 25, 31, 36
- naive(), 7, 19, 21
- numerator_data, 17, 17
- numerator_small, 17
- permute, 18
- plot.klied(dr.histogram), 6
- plot.kmm(dr.histogram), 6
- plot.lhss(dr.histogram), 6
- plot.naivedensityratio(dr.histogram), 6
- plot.spectral(dr.histogram), 6
- plot.ulsif(dr.histogram), 6
- plot_bivariate, 19
- plot_univariate, 20
- predict, 22–25, 27
- predict.klied, 22
- predict.kmm, 23
- predict.lhss, 24

predict.naivedensityratio, 25
predict.spectral, 26
predict.ulsif, 27
print, 28–39
print.kliep, 28
print.kmm, 29
print.lhss, 30
print.naivedensityratio, 31
print.spectral, 32
print.summary.kliep, 33
print.summary.kmm, 34
print.summary.lhss, 35
print.summary.naivedensityratio, 36
print.summary.spectral, 37
print.summary.ulsif, 38
print.ulsif, 39

spectral, 8, 27, 32, 37, 40
stats::approx, 16
stats::density, 16
stats::density(), 16
summary.kliep, 33, 42
summary.kmm, 34, 43
summary.lhss, 35, 44
summary.naivedensityratio, 36, 46
summary.spectral, 37, 47
summary.ulsif, 38, 48

ulsif, 8, 27, 38, 39, 49
ulsif(), 7, 19, 21